Robust Analysis and Design of Bored Pile Considering Uncertain Parameters

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9 Abstract: Many high-rise buildings and bridges in the worlds are constructed using bored pile. To provide a safe design of this type of deep foundation, high quality soil data is needed which 10 11 is normally obtained from laboratory testing. However, the contractor and the consultant often conduct only a limited field testing without performing laboratory tests. As a result, the capacity 12 of bored pile may deviate from the real value. This study aims to develop a framework for 13 analysis and design of axial and lateral capacity of bored piles when only a few soil parameters 14 15 are known. The proposed methodology uses analytical methods backed by numerical calculations according to relevant code of practice. The results indicate that as long as the 16 17 analytical results are supported by the numerical calculations, a robust design can be achieved 18 with only a few soil parameters: a standard penetration test and a cone penetration test.

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20 Key words: Bored pile, axial capacity, lateral capacity, soil properties

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22 **1. Introduction**

Geotechnical engineering is a complex field of construction industry with a massive influence on people's lives. Understanding the principles of geotechnical engineering would ease the construction and design of buildings and reduce possible risks. Various geotechnical issues are encountered in the world: earthquakes, landslides, liquefaction, and soil instability [1-4]. One of major geotechnical failures occurred at the Tokyo Bay Area. Liquefaction and improper design of pile foundation were the main cause of construction failure in this area [5].

The usual role of a deep foundation is to transfer vertical loads through weak soils near the surface to strong soils and rock underneath. Bored pile is one of common types of deep foundation, typically used to accommodate excessive loading from tall buildings [6-7]. Study by Brown et al. [8] indicated that the ranges of diameter and depth of bored piles are 1 m to 2.5

m and 60-90 m, respectively. Bored piles can be constructed using different methods, such as 33 drilling using shafts, drilling under dry condition, installation of caissons and drilled piers [9-34 10]. Axial resistance of bored piles is summation of the based and skin resistances of the piles. 35 The most significant limitation of bored piles is sensitivity of its performance to construction 36 procedure and ground conditions [11-12]. The primary objectives of engineering design are 37 safety, serviceability, and economy. Safety and serviceability can be improved by increasing 38 the safety margins and reducing the probability of failure [13-15]. To develop a framework that 39 40 considers the model uncertainty, a relationship between the parameter, the observation, and the 41 model itself should be clarified [16-18].

Previous studies showed that the Standard Penetration Test (SPT) and the Cone Penetration Test (CPT) were commonly used to determine the required soil properties based on empirical correlation to be used in the geotechnical design [19-21]. Total resistances of pile foundation and bearing capacity of shallow foundation have been correlated directly to these in-situ tests without using tan ϕ ' and c' parameters. To overcome the limitation related to the empirical correlations used in the determination of geotechnical parameters, the European code introduced a partial factor [22-24].

Various theories and models were proposed for geotechnical analysis and design when 49 50 only a few soil properties are known due to limited soil sampling and site investigation. Past 51 studies have been performed to incorporate the uncertainty of soil properties in the slope design. Alkasawneh et al. [25] concluded that limit equilibrium methods, when coupled with the 52 Monte-Carlo searching technique, are efficient to determine the accurate critical slip surface of 53 the slope. Halder et al. [26] studied different analytical approaches and compared them with 54 55 finite element results to determine the accurate factor of safety for various slope angles and soil types. Past research works have also been conducted to incorporate the uncertainty of soil 56 properties in the retaining wall design. Chogueur et al. [27] presents various simulations with 57 the structure installed into the supported ground without surcharge. They concluded that the 58 59 use of computational methods minimizes uncertainties arising from limited number of soil 60 properties. Muñoz-Medina et al. [28] searched for a suitable methodology for the selection of 61 retaining walls for different infrastructures and environments.

Up to date, only a few studies considered the uncertainties in soil properties with respect to foundation. Sakleshpur et al. [29] searched for a method to incorporate uncertain soil properties in the calculation of bearing capacity of shallow foundation. Somantri and Tarigan [30] compared different methods to determine bearing capacity of pile foundation from the results of dynamic analysis. Prayogo et al. [31] also investigated suitable methods to calculate bearing capacity of pile based on the results of dynamic analysis. However, no study has beenconducted to accommodate the uncertainties with respect to bored pile capacity design.

69 The objective of this study is to develop a framework for the design of axial and lateral 70 capacity of bored pile in the area with limited soil parameters. The scope of study includes the 71 analytical calculation using different theories to accommodate the uncertainty due to the 72 limitation of site investigation data. The evaluation of the designed bored pile was carried out 73 using the commercial software for bored pile design.

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75 2. Site Overview and Methodology

The proposed methodology consists of three main steps. In the first step, the properties of the soil were estimated by correlation of SPT and CPT results, as will be discussed in details in Section 3.

79 In the second step, the pile dimensions were estimated considering only its axial resistance. The axial resistance of the pile was calculated using direct and indirect approaches. 80 81 In the former approach, the pile axial capacity was found through correlations of pile shaft and tip resistance with the results of CPT and SPT, while in the latter one the axial capacity was 82 found by substituting the soil properties from the first step into the conventional methods, such 83 as alpha and lambda methods. A comparative analysis was conducted to select the method that 84 85 yielded the most conservative results from the two approaches. The analytical results were further verified by numerical simulations using commercially available software, like GEO5 86 and RSPILE. 87

In the third step, the pile was designed for lateral capacity using three different methods: p-y method, elastic analysis, and Brom's method. The pile-head deflections obtained by three methods were compared to cross-validate the results of analysis. Figure 1 illustrates the methodology.



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Figure 1. Flowchart of research methodology in this study

95 The proposed site is located at the intersection of Santa Monica Boulevard and S Moreno Drive, Los Angeles, USA. The project site is approximately 10,500 m² in plan. The 96 site is flat without any slope. The geotechnical investigation of the site was performed by 97 MACTEC Engineering [32]. The execution and design of project is challenged by the high 98 99 seismicity, strong winds, and presence of deep clay layers at the site. Los Angeles is located at 100 California Cost and is susceptible to severe earthquakes [33]. Over the past hundred years, several powerful earthquakes have struck the region, including the 1999 Hector Mine 101 102 earthquake with a magnitude of 7.1, 1971 San Fernando earthquake with magnitude of 6.6, and 103 1952 Tehachapi earthquake with a magnitude of 7.5. According to data provided by ASCE [34], the speed of wind near the site is approximately 34 m/s for a 50-year mean recurrence interval. 104 Since this value is higher than 30 m/s, the site location qualifies to be a "strong wind zone". 105 Wind direction in Los Angeles varies greatly throughout the year, but the most predominant 106 directions from where wind blows are west (for 4.7 month), north (for 3.9 month), and south 107 (for almost a month) (Weather Spark, n.d.). On average, the wind speed is the highest during 108 109 the winter season, when wind blows mostly from the north; and it is the lowest during summer months, when wind blows mostly from the south direction. 110

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The proposed construction site contains about 15 meters of soft clay layers. This can

be interpreted from cone penetration test result as shown in Figure 2. This type of soil is 112 considered to be problematic in building construction [35]. Clayey soils tend to have low 113 bearing strength and therefore soil improvement or some special considerations in foundation 114 design will be required. In addition, clays are susceptible to shrinkage and volume expansion 115 depending on changes in moisture content, and they also consolidate over a prolonged period 116 of time due to sustained loads. These factors should be properly reflected in the geotechnical 117 design of the building to avoid significant changes in volume which may contribute to a 118 differential soil settlement, cracks in foundation, and permanent damage to the building. 119

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121 **3. Determination of geotechnical parameters**

The geotechnical report, while providing valuable data on soil parameters, lacks certain details. Therefore, it is necessary to correlate missing information from existing data. The basis for majority of the correlations presented in this section were obtained using CPT results. It is well established that CPT results can be used to obtain undrained shear strength, internal friction angle, overconsolidation ratio, coefficient of lateral earth pressure, and many more with a reasonable degree of accuracy [36].

128 The effective friction angle (ϕ') of cohesive soils was assumed to be zero under undrained conditions and vertical loading [37]. The value of ϕ ' for sandy soils was found using 129 four different methods from the values of qc and N₆₀. The definitions of variables presented in 130 Table 1 are as follows: p_a is atmospheric pressure, σ'_0 is the effective stress. The estimated ϕ' 131 of sandy soils in the investigated site is summarized in Table 2. The estimated ϕ' were 132 133 compared with the typical values proposed by Look [38]. If the values of ϕ' were higher than the range of ϕ' provided by Look [38], the values of ϕ' set to maximum ϕ' according to Look 134 [38] for conservative calculation. 135



righte 2. Cone penetration test results from the investigated site



Method №	Equation	Reference
1	$\phi' = \tan^{-1}(0.1 + 0.38\log(\frac{q_c}{\sigma'_o}))$	[39]
2	$\phi' = 27.5 + 9.2\log[N_{60}]$	[40]
3	$\phi' = \sqrt{20N_{60}} + 20$	[41]
4	$\phi' = \tan^{-1} \left(\frac{N_{60}}{\left(12.2 + 20.3 \left(\frac{\sigma'_0}{p_a} \right) \right)} \right)^{0.34}$	[42]

Layer #	Depth interval (m)	Soil type	$egin{array}{c} M_1 \ oldsymbol{\phi}' \end{array}$	$\substack{ M_2 \ \phi' }$	$\substack{{ m M}_3\ m{\phi}'}$	${ m M_4} {oldsymbol{\phi}'}$	Average ϕ'	Typical range (Look, 2007)	Final ϕ' for analysis
2	2 - 4.1	Silty Sand	40	36	33	42	38	37-42	38
6	8 - 11	Silty Sand	32	37	35	36	35	37-42	35
7	11 - 17	Well-graded sand	39	41	45	48	43	40-43	43
12	29.1 - 33.8	Well-graded Sand	40	44	57	51	48	40-43	43
14	35.96 - 37.3	Silty Sand	35	43	50	44	43	37-42	42

Table 2. Result of effective friction angle correlation (M in M1, M2, M3, M4 is abbreviation for Method)

The undrained shear strength of cohesive soils were determined using several methods 141 from CPT results as shown in Table 3. The definitions of variables presented in Table 3 are as 142 follows: s_u is the undrained shear strength, N_k and N_{kt} are the theoretical cone factors, σ_0 is 143 the total stress, q_t is the tip resistance from cone penetration test, f_s is the sleeve resistance 144 from cone penetration test. The typical values of N_k and N_{kt} for normally consolidated clays 145 have been reported to go up to 25 for overconsolidated clays [37]. In this study, upper range 146 147 values were taken for conservative design and analyses. Specifically, Nk was assumed equal to 20 for method 1 and 19 for method 2. The estimated undrained shear strength of cohesive soils 148 is presented in Table 4. As can be seen from the Table 4, the theoretical methods (methods 1 149 and 2) produce consistently higher values of the undrained shear strength as compared to the 150 multi-collinearity model (method 3), even with the application of conservative cone factors. 151 152 Therefore, the estimated undrained shear strength based on method 3 were utilized for conservative design and analyses. 153

Method №	Equation	Reference
1	$s_u = (q_c - \sigma'_0)/N_k$	[43]
2	$s_u = (q_t - \sigma_0) / N_{kt}$	[43]
3	$s_u = 0.070 * (q_t - \sigma_{v0})^{0.846} + 0.390 * f_s$	[44]

Table 3. Summary of correlation methods for undrained shear strength

Layer	Depth interval (m)	Soil type	Method 1 s _u (kPa)	Method 2 s _u (kPa)	Method 3 s _u (kPa)	Final s _u (kPa) for analysis
3	4.1-5.8	Sandy lean clay	163	172	102	102
4	5.8-7.6	Sandy silt	319	340	236	236
5	7.6-8.0	Sandy lean clay	181	201	172	172
8	17-21	Sandy silt	418	439	277	277
9	21-24.4	Clay	260	274	180	180
10	24.4-26.82	Sandy silt	615	646	347	347
11	26.82-29.1	Sandy silt	1061	1110	599	599
13	33.8-35.96	Clay	849	884	515	515
15	37.3-38.1	Sandy silt	471	484	358	358

Table 4. Result of undrained shear strength correlation

The analyses of tip and shaft resistances of piles in sandy soils required earth pressure coefficient (K). The value of K was estimated using method proposed by Kulhawy and Mayne [39]. The estimated K for different sand layers in the investigated site is summarized in Table 5. The estimated K are considerably higher than the typical K values specified in Tomlinson and Woodward [36]. The actual value of K may vary with depth. However, it was decided to use a limiting value of 1.0 for bored piles [36]. This would ensure safe design since high values of K would lead to excessive shaft and toe resistances.

Table 5. Effective earth pressure coefficients for sandy layers

 Layer #	Depth interval (m)	Soil type	Κ	Final K to be used
 2	2 - 4.1	Silty Sand	4.73	1.0
6	8 - 11	Silty Sand	1.75	1.0
7	11 - 17	Well-graded sand	5.73	1.0
12	29.1 - 33.8	Well-graded Sand	7.73	1.0
 14	35.96 - 37.3	Silty Sand	3.56	1.0

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163 The modulus of elasticity of soil (E_s) is a crucial parameter in the analyses of bearing 164 capacity and settlement. This parameter was correlated from CPT and SPT results using Bowles 165 (1996) model. The estimated E_s is summarized in Table 6. The values of estimated E_s were 166 compared with the typical ranges provided by Bowles[45].

Poisson's ratio (v) is a dimensionless ratio that measures the deformation in a material perpendicular to force direction. Typical v is between 0.1 - 0.35 depending on the soil type [38]. The values of v were estimated using a qualitative method proposed by Kulwahy et al. [46].

Layer	Depth interval (m)	Soil type	E _s typical, MPa [45]	E _s based on SPT, (MPa)	E _s based on CPT, (MPa)	Final E _s for analysis, (MPa)
1	0-2.0	Sandy lean clay	15-50	6	8	7
2	2.0-4.1	Silty Sand	7-21	48	48	48
3	4.1-5.8	Sandy lean clay	50-100	7	10	9
4	5.8-7.6	Sandy silt	7-21	7	7	7
5	7.6-8.0	Sandy lean clay	50-100	9	10	10
6	8.0-11.0	Silty sand	7-21	51	21	50
7	11.0-17	Sand	48-81	73	83	83
8	17-21	Sandy silt	7-21	9	9	50
9	21-24.4	Clay	50-100	10	45	50
10	24.4-26.82	Sandy silt	50-100	14	64	64
11	26.82-29.1	Sandy silt	50-100	22	108	108
12	29.1-33.8	Sand	96-192	110	178	196
13	33.8-35.96	Clay	50-100	20	87	87
14	35.96-37.3	Silty Sand	96-192	87	92	92
15	37.3-38.1	Sandy silt	50-100	16	10	50

Table 6. Result of elastic modulus correlation.

171	The pressure sustained by soil per unit deflection was determined by the modulus of
172	subgrade reaction (k_s). Vesic's method [47] was used to determine k_s . Table 7 summarizes the
173	values of all the estimated soil properties.

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Table 7. Summary of the estimated soil properties for geotechnical design of structure.

Interval	Depth interval (m)	Soil Classification	Undrained Shear strength s _{u'}	¢' (°)	σ'0, top kPa	Es, MPa	v	ks, kN/m ³
1	0-2.0	Cohesive (Sandy lean clay)	37.5	-	0	7	0.30	1906
2	2.0-4.1	Cohesionless (Silty Sand)	-	38	36	48	0.20	14542
3	4.1-5.8	Cohesive (Sandy lean clay)	102	-	72	9	0.30	2464
4	5.8-7.6	Cohesive (Sandy Silt)	236	-	102	7	0.30	1906
5	7.6-8.0	Cohesive (Sandy lean clay)	172	-	134	10	0.30	2804
6	8.0-11.0	Cohesionless (Silty Sand)	-	35	140	50	0.25	15565
7	11.0-17	Cohesionless (Sand)	-	43	184	83	0.30	27766
8	17-21	Cohesive (Sandy silt)	277	-	236	50	0.30	16035
9	21-24.4	Cohesive (Clay)	180	-	269	50	0.25	15565
10	24.4-26.82	Cohesive (Sandy silt)	347	-	290	64	0.30	20951
11	26.82-29.1	Cohesive (Sandy silt)	599	-	315	108	0.30	36931
12	29.1-33.8	Cohesionless (Sand)	-	43	337	196	0.35	73045
13	33.8-35.96	Cohesive (Stiff clay)	515	-	375	87	0.30	29219
14	35.96-37.3	Cohesionless (Silty Sand)	-	43	397	92	0.35	32192
15	37.3-38.1	Cohesive (Sandy silt)	358	-	410	50	0.30	16035

176 **4. Axial Capacity of Piles**

Load and resistance factor design (LRFD) method was used in the analysis since the 177 investigated site is located in the USA. A load combination stipulated in California Building 178 Code Section 1605.2 was used in the analysis [48]. The code provides a range of load 179 combinations and requires consideration of the most critical combination. For the case of axial 180 compression, the most critical combination from the code is 1.2(Dead Load) + 1.6(Live Load). 181 The dead and live loads from the upper structure were expected to be 489 kN and 116 kN, 182 respectively [49]. The total factored load on the foundation system is 520 MN. The LRFD 183 184 design requires that factored resistance of piles shall be less than or equal to the sum of shaft 185 resistance and toe resistance multiplied by their respective resistance factors [50].

The geotechnical resistance of piles should not exceed the structural capacity of the 186 piles themselves. In this study, bored concrete piles with the concrete compressive strength of 187 40 MPa, commonly used in industry, were assumed. The structural capacity of the pile (ϕP_n) 188 was calculated following ACI 318 (2014) ignoring contribution of reinforcing steel and 189 assuming tied pile ($\phi P_n = 0.35 f_{cu} A_c$). A combined load factor of 1.4 provided a working load 190 of $0.25 f_{cu}A_c$. The code of practice requires the design of foundation based on the highest load 191 192 from the column acting on a single pile (critical pile). In this study, the critical pile is located 193 at the center of the building. The required factored resistance for the critical pile is 9.63 MN.

194 Given the uncertainties on the soil conditions, a resistance factor of 0.333 [50] for the 195 toe and shaft resistance was adopted. This value corresponds to the lower bound of resistance factors specified in AASHTO code (2007) and produces more conservative results. Two CPT-196 197 based methods were used to calculate the toe and shaft resistances of piles. The first method was originally published by Nottingham and Schmertmann [51] and later improved by 198 Schertmann [52] and included in FHWA-TS-78-209, "Guidelines for Cone Penetration Test, 199 Performance and Design". The second method was adopted based on study by Eslami and 200 Fellenius [53]. Upon completion of the analysis for a given pile diameter and embedment depth 201 using the two methods, the lowest values produced for both the shaft and toe resistance were 202 203 used to calculate the overall nominal bearing capacity of the pile.

In the first method, unit sleeve friction was correlated to nominal shaft resistance (R_s) in cohesionless soil layers using Eq.1. The value of K_s was a function of q_c as well as ratio of embedded pile depth to pile diameter and pile type. The R_s for cohesive soils was determined using Eq. 2. Study by Nottingham [54] indicated that the calculation of the shaft resistance of bored piles using Eq. 2 required the initially obtained nominal resistance taken as two thirds of
its original value. If driven piles are used, this adjustment is not necessary.

 $R_s = K_s f_s A_s \tag{1}$

211 where: K_s – ratio of unit pile shaft resistance to unit sleeve friction, f_s – average unit sleeve 212 friction over a depth interval, A_s – pile shaft surface area over f_s depth interval.

213 $R_s = \alpha' f_s A_s \tag{2}$

214 where: α' – ratio of pile shaft resistance to cone sleeve friction, f_s – average unit sleeve friction 215 over a depth interval, A_s – pile shaft surface area over f_s depth interval.

The pile toe resistance was estimated based on the of averaging of cone resistance values below and above the pile tip. Cone resistance values of 8 pile diameters above and 0.7 to 3.75 pile diameters below the pile tip should be used in the calculation [50]. In this study, an average value of 2.25 ((0.7+3.75)/2) pile diameters below the pile tip was adopted. Schmertmann [52] suggested an upper limit of 15 MPa on the tip resistance. During the averaging procedure, geometric average of values was used as prescribed in AASHTO design manual [55].

In the second method, the shaft resistance was also correlated to the average cone resistance. However, effective cone resistance was used instead of q_c . The unit shaft resistance was calculated using Eq. 3.

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$$f_s = C_s q_E \tag{3}$$

227 where: C_s – shaft correlation coefficient.

The calculation of the unit toe resistance based on the second method was determined in a manner similar to that described in Schmertmann [52]. The difference is that the influence zone at the pile tip ranges from 4b below the pile tip and 8b above where b is the pile diameter/width. The unit toe resistance was calculated using Eq. 4. For pile diameters greater than 16 inches (406 mm), the toe correction coefficient shall be determined from 12/b [50].

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$$q_p = C_p q_E \tag{4}$$

234 where: C_p – toe correction coefficient

The other methods were also used to calculate bearing capacity of the pile based on the soil properties which were determined in Section 3. These methods, often called conventional methods, are summarized in Table 8. Further details can be found in Das (2016).

According to alpha method, the shaft resistance (R_s) of bored pile is found from Eq. 5. The summary of shaft resistances for each clay layer and total resistances within clay layer surrounding pile based on alpha method is presented in Table 9. The value of C in Eq. 6 is suggested as 0.4 - 0.5 for bored piles [37]. In this study, 0.5 was used in the calculation of α following recommendation from American Petroleum Institute [63] for clay material.

$$R_s = \alpha c_u p \Delta L \tag{5}$$

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$$\alpha = C \left(\frac{\sigma'}{c_u}\right)^{0.45} \tag{6}$$

where: c_u – undrained shear strength determined in Section 3, p – perimeter of pile, σ' – average effective vertical stress surrounding the pile, ΔL – thickness of clay layer.

Table 8. Summary of conventional method used to determine pile bearing capacity.

Rs	• Alpha (α) and gamma (γ) method for clays
	• calculation of bearing capacity for sands based on Das (2016)
Rp	Coyle and Castello's methodMeyerhoff's method

Table 9. Shaft resistance based on alpha method for 25 m pile length and 0.5 m diameter.

Interval	Z _{top}	Z _{bot}	$\Delta L(m)$	σ'o, top	c _u kPa	α	Rs, clay
#	(m)	(m)		kPa			kN
3	17	21	4	235.78	276.68	0.465	808.86
4	21	24.4	3.4	268.99	180.04	0.599	575.98
5	24.4	26.82	2.42	290.20	347.27	0.461	608.81
6	26.82	29.1	2.28	315.11	311.00	0.503	560.21
						Σ	2553.87

The determination of shaft resistance of bored pile based on gamma method was found
using Eq.7. The summary of shaft resistance for each clay layer and total resistance within clay
layer surrounding pile based on gamma method is presented in

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The determination of shaft resistance of pile within sandy layers were performed using Eq. 8 (Das, 2016). The value of K = 1 was adopted in this study as explained in Section 3. The soil-pile interaction factor was taken as 0.8 ϕ ' following Das (2016). The summary of shaft resistance for each clay layer and total resistance within clay layer surrounding pile based on lamda method is presented in

258 Table 11.

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Table 10. The gamma factor, *γ*, along pile embedment depth was taken as 0.150 (Das,
2016).

 $R_{\rm s} = \gamma(\sigma' + 2c_{\rm u})p\Delta L$

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The determination of shaft resistance of pile within sandy layers were performed using Eq. 8 (Das, 2016). The value of K = 1 was adopted in this study as explained in Section 3. The soil-pile interaction factor was taken as 0.8 ϕ ' following Das (2016). The summary of shaft resistance for each clay layer and total resistance within clay layer surrounding pile based on lamda method is presented in

Table 11.

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Table 10. Shaft resistance based on gamma method for 25 m long pile and 0.5 m in diameter.

Interval #	z _{top} (m)	z _{bot} (m)	$\Delta L(m)$	σ'o, top	cu (kPa)	γ	Rs, clay
				(kPa)			(kN)
3	17	21	4	235.78	276.68	0.150	759.41
4	21	24.4	3.4	268.99	180.04	0.150	512.45
5	24.4	26.82	2.42	290.20	347.27	0.150	568.60
6	26.82	29.1	2.28	315.11	311.00	0.150	509.35
						Σ	2349.82

 $R_s = K\sigma' tan(\delta')p\Delta L$

(8)

(7)

273 where: δ' – soil-pile interaction factor, K – effective earth pressure coefficient.

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Table 11. Shaft resistance within sand layers for 25 m pile length and 0.5 m diameter.

Interval #	$z_{top}(m)$	$z_{bot}(m)$	$\Delta L(m)$	φ'	δ'	K	$f_s (kN/m^2)$	R _s (kN)
1	8	11	3	35	28	1.0	74.58	351.44
2	11	17	6	42	34	1.0	122.54	1154.88
7	29.1	33.8	4.7	43	34	1.0	230.87	1704.43
							Σ	3210.75

In this study, the toe of the pile was designed to be located within dense sand layer to provide high resistance and to reduce settlement of the building. Therefore, the determination of the toe resistance was conducted using Meyerhof [56] (Equation 9) and Coyle and Castello [57] (Eq. 11). The limiting point resistance, q_L , is given by Eq. 10.

$$R_p = A_p q' N_q^* \le A_p q_L \tag{9}$$

where: q' – effective vertical stress at the pile tip, N_q^* – bearing capacity factor which is a function of friction angle (Das, 2006).

$$q_L = 0.5 \, p_a N_q^* tan \phi' \tag{10}$$

284 where: p_a ' – atmospheric pressure (101.35 kPa)

285

$$R_p = A_p q' N^* \tag{11}$$

where: N^* – bearing capacity factor which is a function of friction angle and the embedment ratio (D/b) (Das, 2006), D – depth of pile, b – diameter of bored pile.

The value of N_q^* for Meyerhof's method was determined_q as 650 from the table in Das 288 [37] for a soil friction angle of 43. Incorporating all required parameters for calculating toe 289 resistance based on Meyerhof's equation, the toe resistance for bored pile with 25 m length and 290 291 0.5 m diameter was 6020 kN. The value of N^* for Coyle and Castello's method was determined as 70. It should be noted that the determination of N^* provides the correlation for internal 292 293 friction angles of up to 40°. Therefore, for all sandy layers where the friction angle was higher than 40° , a curve for 40° was used in the determination of the toe resistance with this method. 294 295 Additionally, for this method, no limit on the toe resistance is stipulated in Das [37]. Therefore, 296 limiting values proposed by Meyerhof [56] for piles in cohesionless soils were used. 297 Incorporating all required parameters for calculating toe resistance based on Coyle and Castello's method, the toe resistance for bored pile with 25 m length and 0.5 m diameter was 298 5145 kN. 299

As can be seen, among the conventional methods, Coyle and Castello's method 300 produces more conservative results for the toe resistance. Therefore, the result from Coyle and 301 302 Castello were utilized as toe resistance of pile and it was combined with the shaft resistance within clay layers from gamma method and the shaft resistance within sand layers from Das 303 [37] method. The total resistance from this conventional method was compared with the total 304 resistance from CPT results. The later method generated the lowest total resistance when 305 306 Eslami and Fellenius [53] method was used. The comparison of total resistance from conventional method and CPT results is presented in Table 12. Compared to the conventional 307 308 methods, the results of CPT-based method are more conservative in this case. With this 309 observation, it was decided to proceed with the entire analysis using CPT-based methods.

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Table 12. Comparisons of total resistance between different methods

Pile diameter	Conventional methods (MN)	CPT based method (MN)
1	11.77	6.54
0.75	7.32	5.09

0.5	3.57	3.54

Overall, five pile diameters were considered in the analysis, i.e. 0.5, 0.75, 1.0, 1.2 and 313 1.65 m. It should be noted that these values are the standard sizes of boring tools which range 314 315 from 600 mm to 2400 mm in 150 mm increment [58]. Figure 3 depicts the results of total resistance. From the figure a pile with a diameter of 1.65 m satisfies the bearing capacity 316 requirement. This pile has a total factored bearing capacity of 11.26 MN (considering one pile 317 per column). The required number of piles for the project was determined assuming a single 318 pile per column. The total structural load was divided by the total resistance and was rounded 319 up to estimate the required number of piles. Figure 4 shows the number of piles versus 320 embedment depth for various design configurations. Upon doing a simple economic analysis 321 based on cost data provided in Hannigan et al. [50], it was observed that group piles were 322 323 uneconomical, and it was decided to proceed with single piled option of 1.65 m diameter pile 324 (Figure 5).

Factored geotechnical resistance (MN)





Figure 3. Variations of total resistance for different penetration depths.





Commercially available GEO5 and RSPILE software [59-60] were used to verify the bearing capacity of the chosen pile. In RSPILE, the soil layers starting from the bottom of the basement were defined according to the soil properties in Table 7. The axial load was applied as factored axial compressive force on top of the pile. The results of the analysis in RSPILE is depicted in Figure 6. As can be seen from the results, upon dividing the ultimate pile capacity

Figure 5. Comparison of cost for construction of foundation using pile group and single pile.

by a safety factor of 3, the allowable capacity is equal to 10.74 MN, which is greater than the

factored load (9.865 MN).

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Figure 6. Results of analyses from RSPILE.

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In a similar manner, all necessary parameters including the pile dimensions, applied 344 loads and water table were defined in GEO5. However, in contrast to defining each soil layer 345 346 as in RSPILE, the digitized version of the CPT results was used. The software calculated the 347 bearing capacity based on the cone tip and sleeve friction values, the results of which can be seen from Figure 7. Table 13 presents a summary of the results obtained by conventional 348 methods, CPT-based methods, and analysis using GEO5 and RSPILE. It is evident from the 349 350 results that the selected pile dimension (D = 1.65 m, L = 25 m) is sufficient to resist the factored axial load effects. 351

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	Calculation of vertical pile bearing capacity - intermediate result
	Pile diameter d _{eq} = 1.65 m
	Pile diameter at base $d_{s,eq} = 1.65 \text{ m}$
	Pile area at base $A_b = 2.14 \text{ m}^2$
	Coeff. of reduc. of pile base bear. capacity $\alpha_p = 0.50$
	Coeff. of influence of pile shape s = 1.00
	Coeff. of influence of pile widened base $\beta = 1.00$
	Calculation of vertical bearing capacity - results
	Analysis carried out for test: Cropped starting from 0
	Pile bearing capacity $F_{r,d}$ = 29917.18 kN
	Pile loading $F_{s,d} = 9685.18 \text{ kN}$
	Safety factor = 3.09>3.00
	Verification of pile for bearing capacity is SATISFACTORY
54	
355	Figure 7. Results of analysis in GEO5
356	
357	
	Table 12 Symmetry of evial bearing consists of sile using working to state
320	rable 15. Summary of axial bearing capacity of pile using multiple methods

	Conventional met hod	CPT-based metho d	Rspile	GEO5 Pile CPT
	16.16 MN	11.26 MN	10.74 MN	9.97 MN
Design geotechni cal capacity	FS=5.0	FS = 3.488	FS = 3.327	FS = 3.089
	ok	ok	ok	ok

5. Lateral Capacity of Piles

This part describes the analysis of the piles for lateral loading. The design procedure for the lateral analysis was adopted from the FHWA manual on drilled shafts [50]. The methodology can be seen from the design flowchart in Figure 8. The results of axial compression design of Section 4 were used for primary sizing of the piles and selection of embedment depth for lateral analysis. The majority of the analysis was performed using the LPILE [61]. With this software all the necessary components outlined in Figure 8 can be calculated. Additionally, non-linear analysis of the pile section using "p-y method" can be performed. This method is recommended for the purposes of lateral analysis of the piles [50]. The p-y method models the shaft as a nonlinear elastic beam and uses a series of nonlinear

- 372 springs to model the soil resistance. This model has been found to capture the essential
- mechanisms of the problem and represent the soil-pile interaction [50].
- 374



375 376

Figure 8. Flowchart for Lateral analysis of Pile

In order to analyze the geotechnical stability of the soil against lateral loads, pile 378 379 pushover analysis was performed. The analysis was done following the guidelines in FHWA manual for drilled shaft foundation [50]. First, the pile shaft was modelled as a simple linear 380 381 elastic beam in LPILE with dimensions from the axial compression design. Uncracked cross section of the pile was assumed. The properties of each soil layer were defined according to 382 the soil properties from Section 3. The built-in p-y curves of the program were used with API 383 sand (O'Neil) curve for cohesionless layers and Stiff Clay with Free Water (Reese) for cohesive 384 layers. These p-y curves are representative of the subsurface characteristics present at the site. 385 386 Once the model was established, to compute the deflections, lateral load was gradually applied at the pile head in multiples up to and exceeding the factored load. A limit set for pile 387

deflection in FHWA manual was checked [50]. Although pile deflection is not the controlling 388 parameter for checking the stability of the pile, the deflection from the analysis should not be 389 greater than 10% of the shaft diameter as specified [50]. The last step in FHWA manual is to 390 check the pile strength. To ensure sufficient strength reserve of the pile, a resistance factor less 391 than one was recommended for lateral resistance. To incorporate this step into the software, 392 393 loads up to $1/\phi$ the factored loads were applied on the pile head, where ϕ is the resistance factor 394 of the soil. According to AASHTO 10.5.5.2.4-1 the recommended value for the factor is 1.0, 395 the FHWA manual suggests a value of 0.67 for p-y method, which was used in this study [50]. 396 The results from the pushover analysis are presented in Figure 9.

From Figure 9, the results of the pushover analysis indicate that the chosen pile dimension (D=1.65m, L= 25m) is sufficient to ensure stability of the soil. In fact, marginal stability was achieved with piles with an embedment depth of 8 meters. However, the 25-meter embedment depth was the required minimum to ensure necessary axial resistance as was explained in Section 4.

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403

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Figure 9. Results of pile pushover analysis

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406 Structural Strength Limit State ensures that the designed shaft had sufficient size and 407 length to withstand the imposed factored loads. In this stage of the analysis, the maximum 408 bending moment and shear force on the pile were determined for the purposes of structural 409 analysis. Additionally, preliminary check of flexural capacity of the pile were made. Similar to 410 axial capacity design, LPILE was used to design of lateral capacity with nonelastic pile section 411 and nominal 1.5% of reinforcement (Figure 10). The parameters for elastic modulus and yield 412 strength of the steel were left as default which were in line with the requirement in this study.
413 No transverse reinforcement was defined for this lateral analysis. The nominal moment
414 capacity of the section as determined by LPILE was 10786 kN-m or 9707 kN-m (including
415 factor) as shown in Figure 11. This value was higher than shear force (1842 kN) and bending
416 moment due to earthquake (7770 kN).

The LPILE can be used to determine the lateral deflection at the pile head. The requirement for the lateral deflection limit was set to 25 mm [50]. Nonlinear pile section was used in the analysis since in many cases a significant component of the deformation can be related to flexural stiffness of the drilled shaft and not the ground response [50]. The result of the analysis in LPILE indicate a pile head deflection of 0.01197 m or 11.97 mm as can be seen from Figure 12.







Figure 10. Nominal shear reinforcement properties for strength check



In order to verify the results produced by LPILE, several other methods were used to check the pile head deflection at service loads. These include the analyses using GEO5 software, Excel spreadsheet, and hand calculation by Brom's method. In all of these alternative methods, a constant value of modulus of subgrade reaction (k_h) was used, which was determined using Vesic's method [62]. Additionally, pinned head conditions was assumed for all calculations to see the maximum theoretically possible head deflections.

The parameters for analysis using GEO5 were defined according to the soil properties 438 stipulated in Section 3 and the pile dimensions were set as previously defined (D=1.65m, 439 L=25m). The Excel spreadsheet provides a solution based on the assumption of elastic pile 440 section with constant EI, constant soil stiffness in each element, and constant subdivision 441 length. 25 elements (1 m per element) were defined in the spreadsheet and the values of k_h 442 443 corresponding to each layer were input. The hand calculation involved the determination of ultimate pile loads and top deflections by Brom's method. It is a simplified method which 444 assumes shear failure in soil for short piles, and bending of pile, governed by the plastic yield 445 446 resistance of the pile section, for long piles. In the analysis, both cases were considered as 447 recommended in the textbook by Das [62].

Table 14 summarizes the results obtained by all of the aforementioned methods. The maximum lateral deflection at the pile head (=11.97 mm) is well below the limit of 25 mm following requirement from FHWA [8]. Therefore, it can be stated the given pile dimensions are enough to satisfy the serviceability criteria. The comparative study indicated that the results from LPILE was higher as compared to results from other methods. It shows that the lateral analyses using LPILE provided more conversative value as compared to other methods.

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- 455

Table 14. Summary of pile head deflections for all analysis methods

	LPILE	GEO5	EXCEL	Das (2010)
y _{max} (mm)	11.97	4.63	7.01	4.77

456

458

457 **6. Conclusions**

The main conclusions of this study are as follows:

The design of bored pile in the area with limited number of soil properties can be carried
out as long as the consultant or contractor has the in-situ testing results from Standard
Penetration Test (SPT) and Cone Penetration Test (CPT).

- 462
 2. The determination of bearing capacity based on the axial load should include the
 463 calculation of skin friction and end bearing capacity using SPT and CPT results as well
 464 as the calculation of total axial capacity using alpha and lambda methods. The most
 465 conservative values from these methods should be used as the determination of the
 466 preliminary dimension of the pile based on the axial capacity
- 467 3. The design of final dimension of the pile should include the effect of the lateral capacity
 468 based on three methods: p-y curve, elastic analysis and Brom's method. The most

- 469 conservative values from these methods should be used as the determination of the final470 dimension of the pile based on the lateral capacity
- 471 4. The appropriate partial factors based on relevant code of practice from USA (FHWA)
 472 should be incorporated in the calculation of bearing capacity of the pile. In this study,
- the results from cone penetration test and standard penetration test with code of practice
 were used to design bored pile with 1.65 m diameter and 25 m depth.
- 475 5. GEO5, APile and LPile can based used to take into account the effect of axial load and
 476 lateral loads in the calculation of bearing capacity.
- 477

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