1 2 3	Effects of Age and Attentional Focus on the Performance and Coordination of the Sit-to- Stand Task
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This study investigated whether age and attentional focus affect synergy organization of sit-tostand (STS), an essential movement for mobility and independence. Young and older adults performed 40 STS trials of STS while holding a cup under internal (IF) and external focus (EF) instructions. Uncontrolled manifold analysis was used to decompose trial-to-trial variability in joint kinematics into variability that preserves (V_{UCM}) and interferes with (V_{ORT}) four control variables: the horizontal and vertical positions of the center of mass (CoM) and the cup. V_{UCM} was significantly higher than V_{ORT} for all control variables in both age groups and focus conditions, indicating concurrent postural and supra-postural synergies. Compared with young adults, older adults demonstrated higher V_{UCM} for all control variables and higher V_{ORT} for all variables except the vertical position of the cup. IF instructions benefited older adults, leading to decreased Vort and thus decreased variability of the vertical position of CoM and the horizontal and vertical positions of the cup. Results suggest that older adults may use higher indices of motor flexibility than young adults to compensate for less accurate control of postural and suprapostural variables. For older adults, IF instructions may improve STS control at the postural and supra-postural levels.

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Keywords: sit-to-stand, attentional focus, aging, uncontrolled manifold

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Introduction

2	Declining performance in the sit-to-stand (STS) task (performed around 60 times per day)
3	(Dall & Kerr, 2010) is a key indicator of reduced mobility in old age and greater risk of falls,
4	hospitalization, and nursing home admission (Makizako et al., 2017; Buatois et al., 2008; Lord
5	et al., 2002; Tinetti et al., 1988). There is, therefore, a significant interest in understanding how
6	mobility tasks of daily living are controlled, how control changes with age, and how control may
7	be improved with rehabilitative interventions.
8	Performance of STS requires coordination of multiple and redundant joint motions across
9	the body to control the displacement of the whole-body center of mass (CoM) from a lower
10	position with a larger base of support (buttocks and feet) to a higher position with a smaller and
11	less stable base (feet). Adequate coordination should produce movements that are stable and
12	flexible enough to produce controlled displacement of the CoM while accommodating changing
13	contextual demands such as varying seat heights, age-related declining muscle strength, or the
14	need to perform a concurrent manual task like keeping a cup of coffee stable during movement
15	(Greve et al., 2019; Hsu, 2014; Hsu & Scholz, 2012). The central nervous system promotes
16	movement stability and flexibility by organizing neuromuscular synergies (Latash & Huang,
17	2015; Latash, 2008; Latash et al., 2002, 2007; Scholz & Schöner, 1999). In the last two decades,
18	the analysis of synergies has been greatly advanced via the uncontrolled manifold (UCM)
19	approach (Latash, 2008; Latash et al., 2007; Reisman et al., 2002; Scholz & Schöner, 1999).
20	In STS, the rising trajectory of the CoM during STS can be generated through a variety of
21	equivalent (redundant) combinations of joint motions. Over repeated STS attempts, joint motions
22	show substantial variability (Scholz et al., 2001). UCM decomposes this variability into two sets:
23	V_{UCM} and V_{ORT} . V_{UCM} is the set of all joint motion values compatible with a stable value of an

important control variable, such as the position of the CoM during STS (Anan et al., 2017; Greve et al., 2013, 2019; Scholz et al., 2001; Scholz & Schöner, 1999). Variability within this set does not affect STS performance; all joint motions within the V_{UCM} set are redundant with respect to the CoM position, and they can be flexibly interchanged from trial to trial. Such variability is good in the sense that it maintains STS stability while affording flexibility (Scholz et al., 2001; Scholz & Schöner, 1999). Therefore, this set is "uncontrolled" (i.e., free to be exploited in order to perform the STS task). In contrast, some combinations of joint motions interfere with the position of the CoM and thus form another set, V_{ORT} (orthogonal to V_{UCM} in mathematical space), that negatively affects performance (Latash et al., 2007; Scholz & Schöner, 1999). This kind of variability should be kept low for adequate STS performance. The relative difference between V_{UCM} and V_{ORT} provides an index of the strength of neuromuscular synergies stabilizing functional movement (Latash et al., 2007). Young and older adults may employ similar multi-joint synergies (V_{UCM} relative to V_{ORT}) to stabilize the CoM during STS (Greve et al., 2013, 2019) and to stabilize the end-point during a goal directed upper extremity reaching task (Greve et al., 2017), but research also suggests that there may be differences in neuromuscular synergies between the two groups (Rosenblatt et al., 2020; Olafsdottir et al., 2007, 2008; Shinohara et al., 2004). For example,= synergies of older adults that stabilize the CoM during balance recovery are less flexible than those of young adults (Hsu et al., 2013), and the synergy index in multi-digit pressing and prehensile tasks is also reduced compared with young adults (Olafsdottir et al., 2007, 2008; Shinohara et al., 2004). In contrast, older adults showed stronger multi-joint synergies stabilizing the swing limb during a cued walking task than young adults (Rosenblatt et al., 2020). Evidence shows that flexible synergistic control allows for multitasking and supra-postural tasks (Hsu, 2014; Hsu & Scholz,

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- 1 2012). A possible consequence of reduced synergy strength is a decreased adaptability in
- 2 accommodating a concurrent manual task during STS (e.g., holding a drink). If older adults show
- 3 less flexible synergies, they may have to prioritize either postural or supra-postural control at the
- 4 expense of the other.
- 5 In the case of reduced synergistic stabilization of movement, rehabilitative interventions
- 6 should promote improvements in STS control. One possible way to modify movement control is
- 7 through cognitive strategies to focus attention (Fietzer et al., 2018; Lohse et al., 2014). For a
- 8 range of skills (e.g., balancing, jumping, throwing), focusing attention on the effects of
- 9 movement on objects or the environment—external focus (EF)—yields better movement
- efficiency (i.e., more fluent, economical, and automatic movements) and effectiveness (i.e., more
- accurate, consistent, and reliable movements) than attending to some aspect of body movement
- itself—internal focus (IF) (Wulf, 2013). The benefits of EF affect performance hypothetically
- through changes in underlying coordination: the "constrained action hypothesis" suggests that IF
- induces a conscious type of control, interfering with automatic coordination processes (Lohse et
- al., 2014; Wulf, 2013), whereas EF can improve coordinative flexibility (Fietzer et al., 2018) by
- prioritizing goal-relevant information for fluid movement coordination (de Melker Worms et al.,
- 17 2017a; Young & Williams, 2014). In dart throwing, for example, EF increases trial-to-trial
- variability of joint motions while improving the accuracy and consistency of dart strike location
- 19 (Lohse et al., 2010). Thus, in UCM terms, an EF could increase covariation of joint motions
- (increase in V_{UCM}) and increase performance accuracy (decrease in V_{ORT}). The benefits of EF
- 21 may also be more pronounced in older adults if EF instructions reduce their greater tendency to
- focus internally on challenging tasks (Mak et al., 2021; Chu & Wong, 2019; Young et al., 2016).
- Holding a cup stable makes for a useful experimental model to test these expectations because it

- 1 creates a natural supra-postural task goal that serves as an external referent to which attention
- 2 may or may not be directed during STS, depending on instructions. Previous studies have shown
- 3 that an EF on a supra-postural task goal increases the accuracy and consistency of postural
- 4 control (Wulf et al., 2003, 2004; McNevin & Wulf, 2002).
- 5 This study investigated synergistic coordination in young and older adults during STS
- 6 while they held a cup under EF and IF conditions. Our first goal was to investigate whether age
- 7 affects synergy organization of STS at the postural and supra-postural levels. In UCM terms,
- 8 differences between young and older adults would be seen in V_{UCM} and V_{ORT} for the CoM and
- 9 cup positions; but, based on the literature, we cannot predict a direction of this difference. Our
- second goal was to determine the effects of EF and IF for young and older adults. Here, we were
- interested in the effect of EF (focus on the cup) or IF (focus on the hand) on CoM and cup
- 12 control during STS. We expected EF to yield more flexible (greater V_{UCM}) and more accurate
- 13 (lower V_{ORT}) CoM and cup control for both age groups, based on the "constrained action
- hypothesis" and previous preliminary findings (Fietzer et al., 2018; Lohse et al., 2010). For older
- adults, we expected a greater difference in favor of EF (thus an interaction effect between age
- and focus) because we expected EF instruction to counteract their tendency to pay deliberate
- attention to their movements (i.e., using IF) when performing challenging tasks (Mak et al.,
- 18 2021; Chu & Wong, 2019; Young et al., 2016).

Methods

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Participants

- A convenience sample of 20 healthy older adults (6 males and 14 females; 69.80 ± 4.57
- years; $25.43 \pm 3.65 \text{ kg/m}^2$) and 26 healthy young adults (6 males and 20 females; 23.00 ± 2.87
- years; $22.40 \pm 2.67 \text{ kg/m}^2$) participated in the study. Inclusion criteria were: (1) be 65 years or

- older or between 18 and 35 years; (2) be right-handed; (3) have normal or corrected-to-normal
- 2 vision; (4) have no musculoskeletal or neurological symptoms affecting STS; and (5) have no
- 3 cognitive disorders affecting the ability to understand and follow instructions. Participants would
- 4 be excluded if they complained of joint pain or could not complete the number of trials required
- 5 for the task. The study protocol followed the Declaration of Helsinki and was approved by the
- 6 local institutional review board. Written informed consent was obtained from all participants.

Equipment and set-up

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- 8 Participants performed STS while holding a cup under EF and IF attention conditions.
- 9 This study focused on the sagittal plane analysis because motion was largely restricted to that
- plane (Scholz & Schöner, 1999). We collected the experimental data with four capture units of
- the Codamotion System (Charnwood Dynamics, Rothley, UK) at a sampling rate of 100 Hz
- 12 (Greve et al., 2013). Marker placement is illustrated in Figure 1. Four-marker rigid clusters were
- attached to the left shank, thigh, forearm, and arm. Three markers were placed on the cup and
- three on the participants' left hand (on the heads of the second and fifth metacarpals and the
- middle of the third metacarpal). Markers were also placed on the left temple, left mastoid
- process, and spinous processes of the seventh cervical, the twelfth thoracic, and the fifth lumbar
- 17 vertebrae. The following landmarks were obtained with a virtual point marker: lateral malleoli,
- 18 lateral epicondyles of the femur, anterior superior iliac spine, great trochanter, acromion, lateral
- 19 epicondyle of the humerus, and the styloid process of the ulnae. The markers were used to define
- virtual segments corresponding to the shank, thigh, pelvis, lower trunk, upper trunk, neck, head,
- arm, forearm, hand, cup, and the intervening joints.
- 22 [Figure 1 near here]

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Experimental procedure

Participants sat on a stool (the height of which was set at 80% of their shank length) holding a cup with their non-dominant hand and resting it on their thigh. The non-dominant hand and a low seat height were chosen because attentional focus effects are more pronounced in more challenging tasks (Landers et al., 2005). In the first trial, participants freely chose the most comfortable initial positions of the buttocks, thighs, feet, and cup. These positions were marked with tape and reproduced in all subsequent trials. Participants performed 45 repetitions of the task at a self-selected comfortable speed while looking at an eye-level target placed on the wall at a distance of 1.3 m (McNevin et al., 2003). By observing participants' gaze, the experimenter ensured that they were looking at the target on every trial. Participants were free to reposition their right hand but were not allowed to push with their hand on the thighs or swing the right arm. Each trial began with a verbal "go" signal. The first five trials had no specific instructions of focus of attention. Participants then performed two blocks of 20 trials each, one for the EF condition and one for the IF condition. Blocks were separated by a 10-minute interval. The order of the blocks (EF-IF or IF-EF) was counterbalanced for each participant to avoid order effects. Instructions were designed to be relevant for real-life situations when one has to stand up with a cup while avoiding liquid spillage. EF instructions were to "focus attention on keeping the cup stable" (inducing a focus outside the body, on the cup) whereas IF instructions were to "focus attention on keeping the hand stable" (inducing a focus internal to the body, on the hand) (Zarghami et al., 2012; Castaneda & Gray, 2007; Parr & Button, 2009). The experimenter reminded participants of the focus instructions after every two trials. After every 10 trials, participants took a 2-minute break, and the experimenter asked them "How well were you able to follow the instructions in the last 10 repetitions?" on a graded scale of 1 (poorly) to 10

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1 (excellently). None of the participants reported fatigue or pain. The data collection session lasted

2 approximately 45 minutes, including preparation.

Data reduction

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4 Marker position data were exported to MATLAB (R2017a, Mathworks, Natick, MA).

Marker position time series were filtered with a 6-Hz low-pass filter (4th order Butterworth).

Cubic spline interpolation was used to estimate marker positions if data were lost for less than 10

consecutive frames. Trials with data gaps greater than 10 frames were discarded. Marker position

was used to calculate segment lengths and joint angles in the sagittal plane (Scholz and Schöner

1999). Joint angles from all trials were visually examined for consistency across repetitions, and

deviant trials were discarded before further analysis. On average, there were 36.54 (\pm 2.17) and

 $38.50 (\pm 1.70)$ good trials per older and young adult, respectively.

The total body center of mass (CoM) position was calculated from position data and anthropometric estimates (Winter, 2009). STS onset and termination were determined automatically and checked visually for all trials. Onset was defined at the point that the CoM horizontal velocity exceeded 5% of its baseline value, before its largest upward deviation. Movement termination corresponded to the last downward deviation of the COM vertical velocity when it crossed the value corresponding to 5% of its baseline. For each trial, the portion from movement onset to termination was normalized to 200 samples in evenly spaced steps with the cubic spline interpolation. STS phases were defined according to Greve et al. (2013) within percentages of the time-normalized trials: preparatory phase (1–30%), lift-off (31–60%), and extension phase (61–100%).

22 STS performance

1 Total movement time was used as a performance indicator for each STS trial. Shorter 2 movement times indicated better performance than longer movement times. Slower movements 3 were expected in older adults (Greve et al., 2013). 4 STS synergies: UCM analysis 5 STS UCM measures were V_{UCM} and V_{ORT} for the horizontal and vertical positions of the 6 CoM and cup. UCM analysis involved three steps (Latash & Zatsiorsky, 2016; Latash et al., 7 2007), which are detailed in Appendix 1. First, the relevant joint angles and the control variables 8 expected to be stabilized by covariation of the joint angles were defined (in the sagittal plane). 9 Second, geometric models (Figure 2 and Appendix 1) linking joint angle changes to control 10 variable changes were defined. Third, projections of variance in the space of elemental variables 11 onto the UCM ($V_{\rm UCM}$) and its orthogonal complement ($V_{\rm ORT}$) were calculated. $V_{\rm UCM}$ and $V_{\rm ORT}$ 12 were calculated at every time frame of STS. The integral of each measure was computed for each 13 of the STS phases (preparatory phase [1%–30%]; liftoff [31%–60%] and extension [61%– 14 100%]). Based on Greve et al. (2013), the analysis focused on the two last phases. 15 [Figure 2 near here] 16 Statistical analyses 17 Statistical analyses were performed using custom RStudio (RStudio, Inc., Boston, MA) 18 scripts. All UCM measures were log-transformed to meet analysis assumptions. For movement 19 time measure, mixed-effects modeling was implemented with age, focus, and their interactions 20 as fixed effects and participant as random effect. Prior to STS coordination analysis, we

time measure, mixed-effects modeling was implemented with age, focus, and their interactions as fixed effects and participant as random effect. Prior to STS coordination analysis, we conducted a preliminary analysis to ensure that V_{UCM} was significantly higher than V_{ORT} . For the preliminary analysis, mixed-effects modeling was implemented with age, type of variance (V_{UCM} or V_{ORT}), phase, and their interactions as fixed effects and participant as random effect. For

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UCM measures, mixed-effects modeling was implemented with age, focus, phase, and their interactions as fixed effects and participant as random effect. A backward stepwise approach was used for model building, as described in West et al. (2015). Models were trimmed by removing nonsignificant effects individually, progressing from higher- to lower-order interactions. The final model only included higher-order interactions that significantly improved model fit and all component lower-order interactions and main effects. Simple-effect analysis and pairwise comparisons were performed to follow up on significant interactions. Degrees of freedom for pairwise comparisons were corrected using the Kenward-Roger method. Alpha was adjusted

9 with the Tukey correction. Level of significance was set at p < .05.

Results

Manipulation check

The average grade answer to the question "How well were you able to follow the instructions in the last 10 repetitions?" for the older adults under EF and IF instructions were 9.8 \pm 0.4 and 9.5 \pm 0.7, respectively. For young adults, the average grade answers were 8.4 \pm 1.4 and 8.1 \pm 1.6, respectively. Although grades of older adults were significantly higher than young adults (F[1;45] = 19.97, p = 0.001, partial $\eta^2 = 0.31$), both age groups followed instructions very well to excellently.

Total movement time

The final model for total movement time revealed no significant main effects or interactions, all ps > .05. Overall, participants took on average 3.13 ± 0.23 seconds to complete each STS repetition.

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STS coordination

- 3 Preliminary analysis
- 4 The final models for horizontal and vertical CoM position, and horizontal cup position
- 5 showed significant age x type of variance and type of variance x phase interactions, all ps <
- 6 .001. The final model for vertical cup position showed significant age x type of variance
- 7 interaction, p < .01. As expected, follow-up pairwise comparisons revealed that V_{UCM} was
- 8 significantly higher than V_{ORT} regardless of age and movement phase for all the four
- 9 coordination variables analyzed, all ps < .01 (Figure 3).
- 10 [Figure 3 near here]
- 11 *V_{UCM}* and *V_{ORT}* for horizontal CoM position
- 12 The final model for V_{UCM} for horizontal CoM position showed significant main effects of
- age, t(45.50) = -2.64, p = .01, and phase, t(131.80) = -6.79, p < .001. V_{UCM} was significantly
- higher for older (M = 0.0065, SD = 0.0037) than young participants (M = 0.0046, SD = 0.0020)
- 15 (Figure 4a), and for phase 2 (M = 0.0063, SD = 0.0031) than phase 3 (M = 0.0046, SD = 0.0027).
- 16 The general patterns of variation of V_{UCM} for horizontal CoM position are shown in Figure 3a.
- 17 The final model for V_{ORT} for horizontal CoM position showed significant main effect of
- age, t(44.20) = -5.07, p < .001 (Figure 4b), and significant focus x phase interaction, t(124.87) =
- 19 2.11, p = .04. Follow-up pairwise comparisons revealed that, although movement phase
- 20 interfered in the direction of V_{ORT} difference, there were no significant differences between focus
- of attention conditions, all ps > .05 (Figure 5a). V_{ORT} was significantly higher for older (M =
- 22 0.0004, SD = 0.0003) than for young participants (M = 0.0002, SD = 0.0001) (Figure 4b). The
- 23 general patterns of variation of V_{ORT} for horizontal CoM position is shown in Figure 3a.

- 1 [Figure 4 near here]
- 2 [Figure 5 near here]
- 3 V_{UCM} and V_{ORT} for vertical CoM position
- 4 The final model for V_{UCM} for vertical CoM position showed significant main effects of
- 5 age, t(45.49) = -2.61, p = .01, and phase, t(131.79) = -7.20, p < .001. V_{UCM} was significantly
- 6 higher for older (M = 0.0064, SD = 0.0037) than young participants (M = 0.0045, SD = 0.0019)
- 7 (Figure 4a), and for phase 2 (M = 0.0062, SD = 0.0031) than phase 3 (M = 0.0045, SD = 0.0026).
- 8 The general patterns of variation of V_{UCM} for vertical CoM position are shown in Figure 3b.
- 9 The final model for V_{ORT} for vertical CoM position showed significant age x focus,
- t(131.75) = 3.67, p < .001, and focus x phase interactions, t(129.99) = 2.05, p = .04. Follow-up
- pairwise comparisons revealed that V_{ORT} was significantly higher when older participants were
- in the EF condition (M = 0.0023, SD = 0.0016) than in the IF condition (M = 0.0016, SD = 0.0016) than in the IF condition (M = 0.0016).
- 13 0.0015), p < .0001 (Figure 5b). This difference between focus was not observed for young
- participants, (EF: M = 0.0010, SD = 0.0007; IF: M = 0.0011, SD = 0.0007), p > .05 (Figure 5b).
- Additionally, V_{ORT} for EF were significantly higher than for IF regardless of age, but only at
- phase 2 (Phase 2: EF: M = 0.0016, SD = 0.0016, IF: M = 0.0011, SD = 0.0008; Phase 3: EF: M = 0.0016
- 17 0.0015, SD = 0.0010, IF: M = 0.0016, SD = 0.0014). The general pattern of variation of V_{ORT} for
- vertical CoM position is shown in Figure 3b.
- 19 [Figure 5 near here]
- V_{UCM} and V_{ORT} for horizontal cup position
- The final model for V_{UCM} for horizontal cup position showed significant main effects of
- age, t(44.41) = -2.45, p = .02, and phase, t(127.82) = -6.05, p < .001. V_{UCM} was significantly
- higher for older (M = 0.0077, SD = 0.0042) than for young participants (M = 0.0055, SD = 0.0042)

- 1 0.0025) (Figure 4a), and for phase 2 (M = 0.0074, SD = 0.0036) than for phase 3 (M = 0.0055,
- SD = 0.0031). The general pattern of variation of V_{UCM} for horizontal cup position is shown in
- 3 Figure 3c.

- 4 The final model for V_{ORT} for horizontal cup position showed significant age x focus x
- 5 phase interaction, t(129.99) = -2.13, p = .03. To follow-up on the age x focus x phase interaction,
- 6 the model was fit separately for each movement phase. Results showed significant age x focus
- 7 interaction, but only for phase 2, t(42.95) = 2.19, p = .03. For phase 2, we found a difference
- 8 between EF and IF, but only for older participants. V_{ORT} was significantly higher for older
- 9 participants in the EF condition (M = 0.0021, SD = 0.0012) than in the IF condition (M = 0.0014,
- SD = 0.0010) (Figure 5c). For phase 3, there was no significant interaction. However, V_{ORT} was
- significantly higher for older (M = 0.0006, SD = 0.0003) than for young participants (M =
- 12 0.0003, SD = 0.0002), t(78.06) = -3.09, p < .01 (Figure 5c). The general pattern of variation of
- 13 V_{ORT} for horizontal cup position is shown in Figure 3c.
- 15 V_{UCM} and V_{ORT} for vertical cup position
- The final model for V_{UCM} for vertical cup position showed significant main effect of age,
- t(61.92) = -2.95, p < .01, and phase, t(130.73) = -6.48, p < .001. V_{UCM} was significantly higher
- 18 for older (M = 0.0078, SD = 0.0043) than for young participants (M = 0.0057, SD = 0.0027)
- 19 (Figure 4a), and for phase 2 (M = 0.0075, SD = 0.0037) than for phase 3 (M = 0.0056, SD = 0.0037)
- 0.0032). The general pattern of variation of V_{UCM} for vertical cup position is shown in Figure 3d.
- 21 The final model for V_{ORT} for vertical cup position showed significant main effect of
- 22 phase, t(128.05) = -4.60, p < .001. V_{ORT} was significantly higher for phase 2 (M = 0.0005, SD = 0.0005)
- 23 0.0003) than phase 3 (M = 0.0004, SD = 0.0002). There was also a significant age x focus

- interaction, t(128.03) = 3.25, p < .01. Follow-up comparisons revealed a difference between EF
- and IF, but only for older participants. V_{ORT} was significantly higher when older participants
- 3 were in the EF condition (M = 0.0005, SD = 0.0003) than when they were in the IF condition (M
- 4 = 0.0004, SD = 0.0003) (Figure 5d). The general pattern of variation of V_{ORT} for vertical cup
- 5 position is shown in F

Discussion

This study employed UCM analysis to investigate synergistic organization of joint angles in the STS of young and older adults while holding a cup and receiving IF or EF instructions. We found evidence for concurrent neuromuscular synergies (Latash et al., 2007) stabilizing both the CoM position, at the postural level, and the cup position, at the supra-postural level. V_{UCM} was consistently higher than V_{ORT} in all movement phases, age groups, and focus conditions for all four control variables analyzed (horizontal and vertical CoM and cup positions, Figure 3). Concerning our first goal, we found evidence that age does affect synergy organization of STS at the postural and supra-postural levels (Figure 4). The possible reduction in synergy flexibility (i.e., lower V_{UCM} values) for older adults compared to young adults was not confirmed by our results. In general, both V_{UCM} and V_{ORT} values were higher for older than for young adults. Concerning our second goal, we found evidence that the focus of attention affects older people differently than young people; however, the evidence did not confirm our expectation that EF

Before discussing age and focus-related differences in synergistic organization, we note that V_{UCM} for the vertical and horizontal as well as V_{ORT} for the horizontal CoM position were significantly higher during lift-off than during the extension phase of STS. This finding is consistent with previous evidence of significantly higher V_{UCM} and V_{ORT} for control of ground

would lead to higher V_{UCM} and lower V_{ORT} values than IF (Figure 5).

- 1 reaction forces (GRF) during the lift-off compared with the extension phase (Greve et al., 2013).
- 2 Lift-off is a critical phase for body coordination during STS because trunk momentum needs to
- 3 be transferred into posterior-anterior and vertical movements of the CoM. In this phase, several
- 4 kinematic adaptations used by older adults such as larger trunk flexion, decreased peak GRF, and
- 5 lower propulsive power imparted to the CoM become evident (Yamada & Demura, 2010;
- 6 Alexander et al., 2001; Gross et al., 1998; Hughes et al., 1994, 1996). Beyond such
- 7 biomechanical adjustments, older adults may also rely on adaptations of interjoint coordination
- 8 during STS task, changing co-variation among lower and upper extremity joints, trunk, and neck
- 9 to seek stability (Greve et al., 2013) and preserve performance. Accordingly, our results show
- that age and focus effects on interjoint coordination measures (V_{UCM} and V_{ORT}) were particularly
- evident during the lift-off phase, while performance measured as total movement time was
- 12 preserved in older adults (no significant difference between groups).

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Our results indicate that, compared with young adults, older adults increase V_{UCM} values for all four control variables (Figure 4a). These results suggest that older adults employ greater motor flexibility, exploring a greater number of equivalent motor solutions leading to the same motor output during STS (Greve et al., 2013). Such increased flexibility is usually interpreted as providing enhanced capacity to perform concurrent tasks, handle new constraints or react to perturbations (Greve et al., 2013; Hsu & Scholz, 2012; Klous et al., 2010; Zhang et al., 2008). However, in older adults, it may not indicate greater potential to better performance, but rather a necessary compensation to deal with age-related functional decline that includes decreases in muscle strength and power (Thompson, 2009; Faulkner et al., 2007), integration of proprioceptive feedback (Goble et al., 2009), coordination of agonist-antagonist muscle pairs (Hortobágyi & Devita, 2006) and cognitive functions involved in postural control (Morris et al.,

- 1 2016; Seidler et al., 2010; Woollacott & Shumway-Cook, 2002). In this sense, increased V_{UCM} 2 may indicate greater use of compensatory mechanisms (Greve et al., 2013). There is preliminary 3 evidence to support this interpretation. Greve et al. (2013) showed that older adults who have 4 low knee extensor muscle strength increased co-variation among the available joint motions to 5 keep GRF stable, although a later study observed that V_{UCM} for CoM position remained 6 unaffected by experimentally increased force or balance demands (Greve et al., 2019). 7 Our V_{ORT} results may also support this interpretation. Unlike previous STS studies 8 (Greve et al., 2013, 2019), we also found increases in V_{ORT} values for all control variables, 9 except the vertical cup position (Figure 4b). Thus, in our task with concurrent postural and supra-10 postural demands, older adults showed more flexible, but more importantly, less accurate joint 11 motion patterns than young adults. Evidence indicates that older adults perform the STS at a 12 much higher percentage of their maximal effort (Greve et al., 2013; Hortobágyi et al., 2003; 13 Alexander et al., 1991, 2001; Gross et al., 1998; Hughes et al., 1996). With increased physical 14 demand, larger sensorimotor noise in the system may cause increased V_{ORT} (Greve et al., 2015). 15 The increase in V_{ORT} (less accurate performance) may be accompanied by a compensatory 16 increase in V_{UCM} as a strategy to preserve stability (preserve the relation between V_{UCM} and 17 V_{ORT}) (Eckardt & Rosenblatt, 2018; Greve et al., 2013, 2015, 2017). Previous studies on the 18 stabilization of the mediolateral trajectory of the swing limb during gait (Eckardt & Rosenblatt, 19 2018), center of pressure displacement in quiet standing (Freitas & Duarte, 2012), and CoM 20 during balance recovery (Hsu et al., 2013) also report increased V_{ORT} for older compared with 21 young adults. 22
 - Next, we consider the observed effects of attentional focus on performance and synergistic coordination measures. Contrary to our expectations, the EF showed no beneficial

increase in V_{UCM} or reduction in V_{ORT}. Surprisingly, the IF instruction benefited older adults 1 2 during the lift-off phase, leading to decreased V_{ORT} and thus decreased variability of the vertical 3 CoM position and the horizontal and vertical cup positions. In contrast, young adults were not 4 affected by focus instructions (Figure 5). The observed IF advantage in older adults' postural and 5 supra-postural control runs counter to the well-documented advantages of EF and disadvantages 6 of IF for motor performance (McNevin et al., 2003; Wulf, 2013; Wulf et al., 2004). This 7 unexpected result cannot be explained by low adherence to instructions because both young and 8 older adults reported following instructions very well or excellently but may be related to the 9 nature of the STS. We speculate that general postural and mobility skills that are acquired 10 spontaneously during normal motor development with little declarative instruction (phylogenetic 11 skills such as the STS) are less vulnerable to the usual negative interferences of an IF (de Melker 12 Worms et al., 2017a; Young & Williams, 2015). 13 Evidence supports this speculation. One previous study failed to find any detrimental 14 effects of IF or beneficial effects of EF on the performance of the STS while holding a cup at the 15 level of movement outcomes: STS duration and cup angle, stability, and smoothness (Pinto et al., 16 2020). It is possible that IF has negative effects only for specialized, complex movement skills 17 usually acquired with great amounts of explicit instruction in early practice. For these tasks, IF 18 may revert the individual to an earlier declarative stage of learning and interfere with the 19 automaticity of control, while EF might prioritize relevant, goal-related information for fluent 20 coordination (de Melker Worms et al., 2017a; Young & Williams, 2014). Also, despite some 21 previous research showing benefits of EF for posture and mobility skills (Richer, et al., 2017; 22 Chiviacowsky et al., 2010; McNevin et al., 2013;), our results are consistent with more recent 23 studies that report null effects for focus instructions for day-to-day posture and mobility skills

- 1 (Monahan & Hurley, 2021; Mak et al., 2020; Chow et al., 2019; de Melker Worms et al., 2017a,
- 2 2017b; Richer et al., 2017; Yogev-Seligmann et al., 2017; Landers et al., 2016; De Bruin et al.,
- 3 2009).
- 4 Possible reasons for the beneficial effects of the IF for older adults are unclear. An
- 5 optimal individual attentional strategy may depend on motor imagery ability and personal
- 6 preferences (Sakurada et al., 2016, 2017; Maurer & Munzert, 2013). Focusing internally may
- 7 have been a more familiar, less attention-demanding strategy for older adults. Our observation
- 8 that an IF may benefit postural and supra-postural control for older adults is a novel finding that
- 9 merits further investigation, especially with respect to the possibility of improving the postural
- performance through dual-task practice wherein IF is applied to the control of supra-postural
- 11 motor task.

12 Study limitations might have influenced the results. The use of an empty cup may not 13 have made the task challenging enough for a beneficial effect of EF to emerge (Landers et al., 14 2005). Also, although participants reported following instructions very well to excellently, they 15 were not asked about their actual attentional content. Different results at the level of the 16 synergistic control of STS might have been found, had these variables been manipulated or 17 controlled for. However, a recent study that increased STS difficulty by using a full cup with 18 added speed demands and controlled for attentional content failed to reveal any beneficial effects 19 of an EF at the level of performance. Interestingly, an IF was associated with better cup accuracy 20 (lower variability of the inclination angle) during stand-to-sit, both for young and older adults 21 (Pinto et al., 2020). It is also worth mentioning that joint angle measurement is a challenge for 22 the field of motor control. The computation of joint angle variance within and orthogonal to the

UCM assumes that the human body can be adequately represented as a set of rigid body elements

1	connected by joints. Methodological studies investigating the precision of joint angle estimates
2	based on this assumption would be valuable.
3	
4	Conclusions
5	This study found evidence for control of the STS with concurrent neuromuscular
6	synergies stabilizing both the CoM at the postural level, and the cup position at the supra-
7	postural level. Our findings and previous studies on age differences in motor flexibility during
8	STS and other tasks provide evidence that there is not a general decline in motor flexibility with
9	aging. Rather, older adults may use higher indices of motor flexibility than young adults to
10	compensate for less accurate control of postural and supra-postural variables. Contrary to
11	expectations, for older adults, STS control may be improved both at the postural and supra-
12	postural levels by IF rather than EF instructions.
13	
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19	
20	Disclosure of interest
21	The authors report there are no competing interests to declare.
22	
23	Data availability statement

1 The data that support the findings of this study are available from the corresponding author, VA, upon reasonable request. 2 3 4 References 5 Alexander, N. B., Gross, M. M., Medell, J. L., & Hofmeyer, M. R. (2001). Effects of functional 6 ability and training on chair-rise biomechanics in older adults. Journals of Gerontology -7 Series A Biological Sciences and Medical Sciences, 56(9), M538–M547. 8 https://doi.org/10.1093/gerona/56.9.M538 9 Alexander, N. B., Schultz, A. B., & Warwich, D. N. (1991). Rising from a chair: Effects of age 10 functional ability on performance biomechanics. *Journals of Gerontology*, 46(3), 91–98. 11 https://doi.org/10.1093/geronj/46.3.m91 12 Anan, M., Hattori, H., Tanimoto, K., Wakimoto, Y., Ibara, T., Kito, N., & Shinkoda, K. (2017). 13 The coordination of joint movements during sit-to-stand motion in old adults: the 14 uncontrolled manifold analysis. *Physical Therapy Research*, 20(2), 44–50. 15 https://doi.org/10.1298/ptr.E9923 16 Buatois, S., Miljkovic, D., Manckoundia, P., Gueguen, R., Miget, P., Vançon, G., Perrin, P., & 17 Benetos, A. (2008). Five times sit to stand test is a predictor of recurrent falls in healthy 18 community-living subjects aged 65 and older. Journal of the American Geriatrics Society, 19 56(8), 1575–1577. https://doi.org/10.1111/j.1532-5415.2008.01777.x 20 Castaneda, B., & Gray, R. (2007). Effects of focus of attention on baseball batting performance 21 in players of differing skill levels. *Journal of Sport and Exercise Psychology*, 29(1), 60–77. 22 https://doi.org/10.1123/JSEP.29.1.60 23 Chiviacowsky, S., Wulf, G., & Wally, R. (2010). An external focus of attention enhances

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Appendix 1: UCM Analysis

1 The angles for ankle, knee, hip, lumbar spine, thoracic spine, cervical spine, atlanto-2 occipital, sternoclavicular, shoulder, elbow, wrist and hand-cup (the angle between the vector from 3 the 2nd metacarpophalangeal to the wrist joint and the vector between the two markers in the cup) 4 were defined in the sagittal plane. Control variables that were expected to be stabilized by co-5 variation of joint angles during STS were defined. The vertical and horizontal position of the CoM 6 in the sagittal plane were the two main control variables (Scholz et al., 2001; Scholz & Schöner, 7 1999). The bidimensional cup position in the sagittal plane was also considered a potentially 8 stabilized control variable. Geometric models linking joint angle changes to control variable 9 changes were defined with the angles: $\theta 1=$ ankle, $\theta 2=$ knee, $\theta 3=$ hip, $\theta 4=$ lumbar spine, $\theta 5=$ 10 thoracic spine, $\theta = \theta$ cervical spine, $\theta = \theta$ atlanto-occipital, $\theta = \theta$ sternoclavicular, $\theta = \theta$ shoulder, $\theta = \theta$ 11 elbow, $\theta 11 = \text{wrist}$, and $\theta 12 = \text{hand-cup}$.

12

A. Geometric model relating horizontal Cup horizontal position (*Cup hor*) to joint configuration space:

B. Geometric model relating horizontal Cup vertical position (*Cup vrt*) to joint configuration space:

```
+l11\sin(\theta_1+\theta_2+\theta_3+\theta_4+\theta_5+\theta_8+\theta_9+\theta_{10}+\theta_{11})
                   1
                 2
                                                                                                                                                                               +l12\sin(\theta_1+\theta_2+\theta_3+\theta_4+\theta_5+\theta_8+\theta_9+\theta_{10}+\theta_{11}+\theta_{12})
                 3
                                                                               C. Geometric model relating horizontal CoM position (CoM hor) to joint configuration space
               4
               5
                                                                                                                                                                               COM \text{ hor} = origin pos \text{ hor} + m1(l1 \cos(\theta 1) r1)
               6
                                                                                                                                                                               + m2(l1\cos(\theta 1) + l2\cos(\theta 1 + \theta 2)r2)
               7
                                                                                                                                                                               +m3(l1\cos(\theta 1)+l2\cos(\theta 1+\theta 2)+l3\cos(\theta 1+\theta 2+\theta 3)r3)
               8
                                                                                                                                                                               +m4(l1\cos(\theta 1)+l2\cos(\theta 1+\theta 2)+l3\cos(\theta 1+\theta 2+\theta 3)+l4(\theta 1+\theta 2+\theta 3+\theta 4)r4)
               9
                                                                                                                                                                               + m5(l1\cos(\theta 1) + l2\cos(\theta 1 + \theta 2))
   10
                                                                                                                                                                               +l3\cos(\theta_1+\theta_2+\theta_3)+l4\cos(\theta_1+\theta_2+\theta_3+\theta_4)+l5\cos(\theta_1+\theta_2+\theta_3+\theta_4+\theta_5)r5
   11
                                                                                                                                                                               + m6 (l1 \cos(\theta 1))
   12
                                                                                                                                                                               + l2 \cos(\theta 1 + \theta 2) + l3 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 3) + l4 \cos(\theta 1
   13
                                                                                                                                                                               +\theta 2+\theta 3+\theta 4+\theta 5) +l6cos(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6)r6) +m7(l1cos(\theta 1)
   14
                                                                                                                                                                               + l2 \cos(\theta 1 + \theta 2) + l3 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 3) + l4
   15
                                                                                                                                                                               +\theta 2+\theta 3+\theta 4+\theta 5)+l6cos(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6)
   16
                                                                                                                                                                               +l7\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4}+\theta_{5}+\theta_{6}+\theta_{7})r7
   17
                                                                                                                                                                               + m8(l1\cos(\theta 1)
   18
                                                                                                                                                                               + l2 \cos(\theta 1 + \theta 2) + l3 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 3) + l4
   19
                                                                                                                                                                               +\theta 2+\theta 3+\theta 4+\theta 5)+l8\cos(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7+\theta 8)r8)
 20
                                                                                                                                                                               + m9(l1\cos(\theta 1)
21
                                                                                                                                                                               + l2 \cos(\theta 1 + \theta 2) + l3 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 3) + l4
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                                                                                                                                                                               +\theta 2+\theta 3+\theta 4+\theta 5)+l8\cos(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7)
                                                                                                                                                                               +\theta 8)+l9\cos(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7+\theta 8+\theta 9)r9)
23
24
                                                                                                                                                                               +m10(l1\cos(\theta 1)
 25
                                                                                                                                                                               + l2 \cos(\theta 1 + \theta 2)
                                                                                                                                                                               +l3\cos(\theta_{1}+\theta_{2}+\theta_{3})+l4\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l5\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4})+l6\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4}+\theta_{4}+\theta_{3}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}+\theta_{4}
 26
                                                                                                                                                                               +\theta 2+\theta 3+\theta 4+\theta 5) +l8\cos(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7)
27
 28
                                                                                                                                                                               +\theta 8)+l9\cos(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7+\theta 8+\theta 9)
                                                                                                                                                                               +l10\cos(\theta_1+\theta_2+\theta_3+\theta_4+\theta_5+\theta_6+\theta_7+\theta_8+\theta_9+\theta_{10})r_{10})+m_{11}(l_1\cos(\theta_1)+\theta_1)r_{10}
 29
                                                                                                                                                                               + l2 \cos(\theta 1 + \theta 2) + l3 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 2 + \theta 3) + l4 \cos(\theta 1 + \theta 3) + l4
 30
                                                                                                                                                                               +\theta 2+\theta 3+\theta 4+\theta 5) +l8\cos(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7)
   31
 32
                                                                                                                                                                               +\theta 8)+l9\cos(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7+\theta 8+\theta 9)
                                                                                                                                                                               +l10\cos(\theta_1+\theta_2+\theta_3+\theta_4+\theta_5+\theta_6+\theta_7+\theta_8+\theta_9+\theta_{10})
 33
   34
                                                                                                                                                                               +l11\cos(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4}+\theta_{5}+\theta_{6}+\theta_{7}+\theta_{8}+\theta_{9}+\theta_{10})
 35
                                                                                                                                                                               + \theta 11)r11)
 36
 37
 38
 39
 40
41
42
43
 44
 45
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1
                                                                                       C. Geometric model relating vertical CoM position (CoM vrt) to joint configuration space:
                 2
                 3
                                                                                                                                                                                                COM\ vrt = origin\ pos\ vrt + m1(l1\sin(\theta 1)r1)
                 4
                                                                                                                                                                                                + m2(l1 \sin(\theta 1) + l2 \sin(\theta 1 + \theta 2) r2)
                 5
                                                                                                                                                                                                +m3(l1\sin(\theta 1)+l2\sin(\theta 1+\theta 2)+l3\sin(\theta 1+\theta 2+\theta 3)r3)
                 6
                                                                                                                                                                                                +m4(l1\sin(\theta 1)+l2\sin(\theta 1+\theta 2)+l3\sin(\theta 1+\theta 2+\theta 3)+l4\sin(\theta 1+\theta 2+\theta 3+\theta 4)r4)
                   7
                                                                                                                                                                                                + m5(l1 \sin(\theta 1) + l2 \sin(\theta 1 + \theta 2)
                 8
                                                                                                                                                                                                +l3\sin(\theta_1+\theta_2+\theta_3)+l4\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4+\theta_5)r5
                 9
                                                                                                                                                                                                +m6 (l1 \sin(\theta 1))
                                                                                                                                                                                                + l2 \sin(\theta 1 + \theta 2)
    10
                                                                                                                                                                                                +l3\sin(\theta_1+\theta_2+\theta_3)+l4\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l5\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_2+\theta_3+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4)+l6\sin(\theta_1+\theta_4
    11
    12
                                                                                                                                                                                                +\theta 2+\theta 3+\theta 4+\theta 5) +l6sin(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6)r6) +m7(l1sin(\theta 1)
    13
                                                                                                                                                                                                + l2 \sin(\theta 1 + \theta 2) + l3 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 3) + l4 \sin(\theta 1
                                                                                                                                                                                                +\theta 2+\theta 3+\theta 4+\theta 5)+l6sin(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6)
    14
    15
                                                                                                                                                                                                +l7\sin(\theta_1+\theta_2+\theta_3+\theta_4+\theta_5+\theta_6+\theta_7)r7
    16
                                                                                                                                                                                                + m8(l1 \sin(\theta 1))
                                                                                                                                                                                                + l2 \sin(\theta 1 + \theta 2) + l3 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 3) + l4 \sin(\theta 1
    17
    18
                                                                                                                                                                                                +\theta 2+\theta 3+\theta 4+\theta 5)+l8\sin(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7+\theta 8)r8)
    19
                                                                                                                                                                                                + m9(l1 \sin(\theta 1))
  20
                                                                                                                                                                                                + l2 \sin(\theta 1 + \theta 2) + l3 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 3) + l4 \sin(\theta 1
21
                                                                                                                                                                                                +\theta 2+\theta 3+\theta 4+\theta 5)+l8\sin(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7)
22
                                                                                                                                                                                                +\theta 8)+l9\sin(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7+\theta 8+\theta 9)r9)
  23
                                                                                                                                                                                                + m10(l1 \sin(\theta 1))
  24
                                                                                                                                                                                                + l2 \sin(\theta 1 + \theta 2) + l3 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 2 + \theta 3) + l6 \sin(\theta 1 + \theta 3) + l6
                                                                                                                                                                                                +\theta 2+\theta 3+\theta 4+\theta 5) +l8\sin(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7)
25
                                                                                                                                                                                                +\theta 8)+l9\sin(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7+\theta 8+\theta 9)
  26
27
                                                                                                                                                                                                +l10\sin(\theta_1+\theta_2+\theta_3+\theta_4+\theta_5+\theta_6+\theta_7+\theta_8+\theta_9+\theta_{10})r10) + m11(l1\sin(\theta_1)
28
                                                                                                                                                                                                + l2 \sin(\theta 1 + \theta 2) + l3 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3 + \theta 4) + l5 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 2 + \theta 3) + l4 \sin(\theta 1 + \theta 4) + l4 \sin(\theta 1
  29
                                                                                                                                                                                                +\theta 2+\theta 3+\theta 4+\theta 5) +l8\sin(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7)
  30
                                                                                                                                                                                                +\theta 8)+l9\sin(\theta 1+\theta 2+\theta 3+\theta 4+\theta 5+\theta 6+\theta 7+\theta 8+\theta 9)
  31
                                                                                                                                                                                                +l10\sin(\theta_1+\theta_2+\theta_3+\theta_4+\theta_5+\theta_6+\theta_7+\theta_8+\theta_9+\theta_{10})
    32
                                                                                                                                                                                                +l11\sin(\theta_{1}+\theta_{2}+\theta_{3}+\theta_{4}+\theta_{5}+\theta_{6}+\theta_{7}+\theta_{8}+\theta_{9}+\theta_{10})
  33
                                                                                                                                                                                                + \theta 11)r11)
  34
  35
```

origin pos hor is the horizontal position of the origin, i.e. the ankle, origin post vrt is the vertical position of the origin, i.e. the ankle, li is the segment length where i={shank, thigh, pelvis, lower trunk, upper trunk, neck, head, clavicle, upper arm, forearm, hand, hand-cup, great trochanter to acromion}, mi is the mass proportion of the segment, ri is the length proportion of the segment CoM to distal reference point, and θi is the angle between segments.

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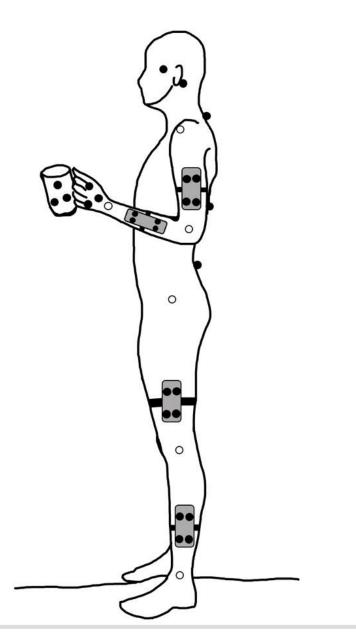
41

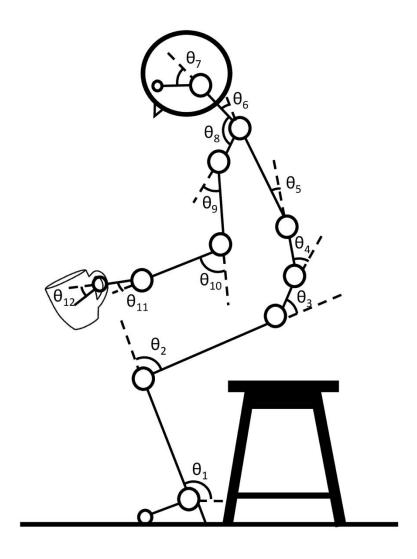
42

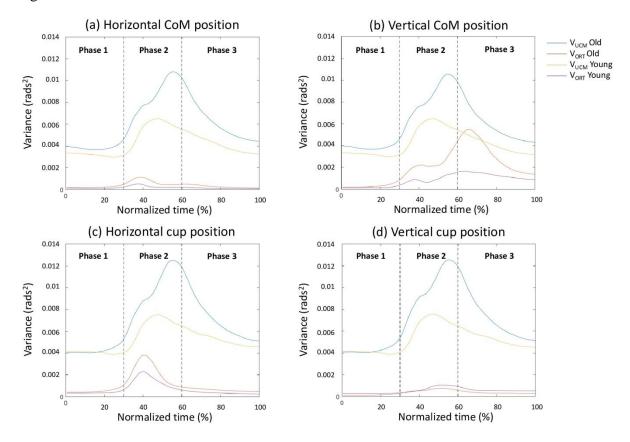
Finally, projections of variance in the space of elemental variables onto the UCM (V_{UCM}) and onto its orthogonal complement (V_{ORT}) were calculated. Magnitudes of V_{UCM} and V_{ORT} were normalized by the number of dimensions in the corresponding subspaces so they could be

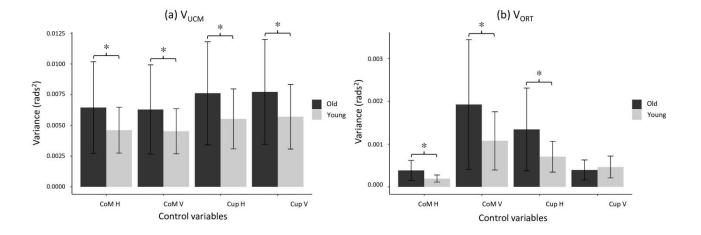
compared quantitatively. V_{UCM} and V_{ORT} were calculated at every time frame of STS. The integral of each measure was computed for each of the three STS phases.

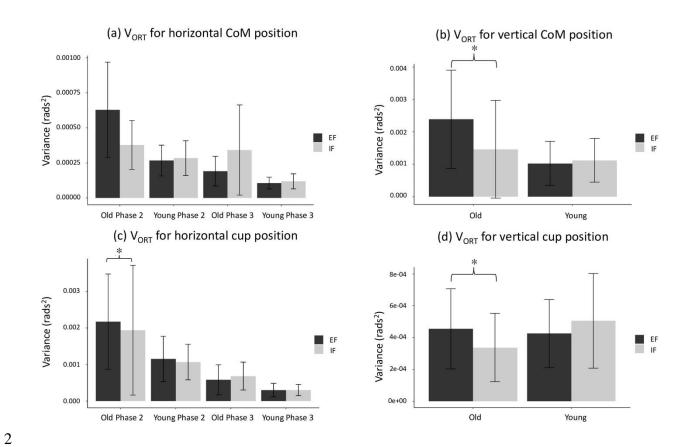
1 Figure 1 2











1 Figure 1. Schematic of the experimental set-up with clusters, active markers (filled circles) and 2 virtual markers (empty circles). 3 4 Figure 2. Geometric model linking joint angles to changes in the control variables. The 12 angles 5 used in the Jacobian matrices were (from Θ_1 to Θ_2): ankle, knee, hip, lumbar-spine, thoracic-6 spine, cervical-spine, atlanto-occipital, sternoclavicular, shoulder, elbow, wrist, and hand-cup 7 angle. 8 9 Figure 3. Average V_{UCM} and V_{ORT} values over time as a function of age for (a) horizontal and (b) 10 vertical CoM positions, and (c) horizontal and (d) vertical cup positions. 11 12 Figure 4. Mean (a) V_{UCM} and (b) V_{ORT} values for the horizontal and vertical CoM and cup 13 positions as a function of age. Asterisk (*) indicates p < .05. Error bars represent standard 14 deviation of the mean. H = horizontal; V = vertical. 15 16 Figure 5. Mean V_{ORT} values for (a) the horizontal CoM and (c) cup positions as a function of 17 focus of attention, age, and movement phase; and mean V_{ORT} values for (b) the vertical CoM and (d) cup positions as a function of focus of attention and age. Asterisk (*) indicates p < .05. Error 18 19 bars represent standard deviation of the mean.