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## Associative vs. dissociative binding of CO<sub>2</sub> on M<sub>4</sub> transition metal clusters

Sherfi Sherif, Bala Aakash Velmurugan, Naeem Abbas, Muskanbanu Shaikh and Matthew A. Addicoat  \*

Density functional theory calculations were performed to determine reaction paths for the reaction of CO<sub>2</sub> with M<sub>4</sub> transition metal clusters (M = Nb, Mo, Ru, Rh, Pd, Ag, Pt). Geometries incorporating associatively bound (CO<sub>2</sub>), partly dissociated (O + CO) and fully dissociated (O + C + O) carbon dioxide were identified for all clusters except Ag<sub>4</sub>. Nb<sub>4</sub> and Mo<sub>4</sub> are likely to dissociate CO<sub>2</sub> fully. For Ru<sub>4</sub>, both partly and fully dissociative geometries were competitive, while Rh<sub>4</sub>, Pd<sub>4</sub> and Pt<sub>4</sub> activate CO<sub>2</sub> without breaking either CO bond. Ag<sub>4</sub> was found to interact only minimally with CO<sub>2</sub>. The change in  $\nu_{\text{bend}}$ , the energy of the CO<sub>2</sub>  $\pi_u$  orbital in the physisorbed M<sub>4</sub>CO<sub>2</sub> capture species and the charge transfer to the CO<sub>2</sub> molecule,  $q(\text{CO}_2)$ , in the first transition state were found to correlate with the eventual fate of the CO<sub>2</sub> molecule.

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## 1 Introduction

Carbon dioxide CO<sub>2</sub>, is one of the key pollutant gasses contributing to global warming and ocean acidification.<sup>1</sup> In recognition of the urgency of this problem, in recent years there have been increasing efforts to develop and deploy carbon capture and storage systems. To go one step further, rather than storing carbon captured from the atmosphere (as CO<sub>2</sub>), valorizing it as a C<sub>1</sub> feedstock. Captured CO<sub>2</sub> could be used to produce common feedstock chemicals and fuels such as formaldehyde, methanol and formic acid.<sup>2,3</sup> Reduction of CO<sub>2</sub> *via* the reverse Water Gas Shift (rWGS) reaction produces carbon monoxide, CO, that can be employed in a variety of industrially relevant reactions.<sup>4,5</sup>

Somewhat frustrating the aim of employing captured CO<sub>2</sub> as a reactant in various chemical processes, is its exceptional thermodynamic and kinetic stability: the Gibbs free energy of formation,  $\Delta_f G$  at 298 K is  $-394.36 \text{ kJ mol}^{-1}$ .<sup>6</sup> Therefore, activating the CO<sub>2</sub> molecule, by partly or fully breaking one of the two C=O bonds requires one or more of; a careful choice of reactants that can donate to the CO<sub>2</sub> molecule, a similarly careful choice of product, shifting the equilibrium – *e.g.* by removing product, and a large energy input.<sup>7</sup>

Considering the mechanism of how a catalytic system can activate CO<sub>2</sub>, upon CO<sub>2</sub> adsorption or coordination to the system, often at the site of a metal centre, electron density is introduced into the antibonding  $\pi^*$  orbitals of CO<sub>2</sub>. The C=O bonds are thereby weakened and the molecule subsequently

adopts a bent geometry ( $\theta_{\text{OOC}} \approx 120\text{--}140^\circ$ ), creating a dipole and increasing the reactivity of CO<sub>2</sub>.<sup>7–11</sup>

A variety of novel catalysts for the activation of CO<sub>2</sub> have been proposed, including MOFs,<sup>12–14</sup> ceria<sup>15,16</sup> and a variety of metal (oxide) surfaces including Fe<sup>17</sup>, Ti<sup>18</sup>, Cu<sup>19</sup> and Pd/Mo.<sup>20</sup> A key feature of all of these proposed catalysts is that they involve one or more metal atoms at the active site as the source of the electron density donated to the CO<sub>2</sub> molecule.

Transition metal clusters have been studied both experimentally and computationally for many years for their capacity to adsorb and activate various small molecules including CO<sub>2</sub>.<sup>21,22</sup> Transition metal clusters were initially studied as models of bulk surfaces.<sup>23</sup> However, it was rapidly identified that the properties of these clusters is both size<sup>24</sup> and geometry-dependent,<sup>25,26</sup> and therefore, that by modifying the size and composition of the (nano)clusters, that the properties, especially the reactivity, of the clusters could be tuned.<sup>23,27,28</sup> Most recently, transition metal clusters have been confined within the pockets of porous framework materials, with the goal of protecting the active metal clusters from sintering, whilst the porous framework still allows mass transfer.<sup>29,30</sup>

Computational studies, normally employing density functional theory (DFT), are key in determining the geometric structures and reaction mechanisms in both gas-phase<sup>31–33</sup> and surface studies,<sup>34</sup> especially identifying where barriers may prevent thermodynamic products from being observed.<sup>35</sup> A recent DFT-based mechanistic study from Mondal *et al.* showed that beyond simply the static cluster geometry, the fluxionality of the cluster was important in determining the reduction of CO<sub>2</sub> on supported copper tetramers.<sup>36</sup> Da Silva and coworkers studied the reverse water gas shift reaction on

School of Science and Technology, Nottingham Trent University, Clifton Lane, Nottingham, NG11 8NS, UK. E-mail: matthew.addicoat@ntu.ac.uk



series of  $M_{13}$  clusters,  $M = Fe-Cu$  and observed that increasing the d-state occupation favoured COOH formation.<sup>5</sup> Recently, Mohanta and Jena attempted to address the poor selectivity of the  $Cu_{13}$  cluster by investigating a series of  $XCu_{12}$  clusters, where X was a variety of first and second row transition metal atoms.

With a similar aim of understanding cluster behaviour across the periodic table, in this work, we present DFT calculated reaction paths for  $CO_2$  addition to second row  $M_4$  transition metal clusters from  $Nb_4$  to  $Ag_4$ , we exclude technetium, due to its radioactivity, but we include the third-row  $Pt_4$  cluster due to the popularity of platinum as a catalyst.

## 2 Computational method

Structures of  $M_4$  clusters, for  $M = Nb-Ag$  (excluding  $Tc$ ) and  $Pt$  were generated using the Kick stochastic structure search procedure with four individual  $M$  atoms supplied.<sup>37,38</sup> Full searches were undertaken on the lowest possible multiplicity (singlet for all  $M_4$  clusters) and all minima identified were re-optimized at higher multiplicities. For all species, the lowest four multiplicities were calculated, but for rhodium, palladium and platinum, the search was extended up to the nonet. Ruthenium is known to have low lying minima with high numbers of unpaired electrons and so the search was further extended up to the 15-tet. No symmetry was imposed at any point in the search, nevertheless, several clusters adopted clear point group symmetry, as evidenced by geometric parameters and frequencies. Where point group symmetry was observed in either bare  $M_4$  or  $M_4CO_2$  clusters, we refer to this apparent symmetry, but we did not confirm the symmetry by further constrained calculation, as the addition of  $CO_2$ , or further steps on the reaction path would immediately break symmetry.

The lowest energy structure of each  $M_4$  cluster was then adopted as a fragment in a further stochastic search process. Kick runs were undertaken searching for with the following configurations:  $M_4 + CO_2$  (*i.e.* intact  $CO_2$ );  $M_4 + CO + O$ ;  $M_4 + C + O + O$ . As activation of the  $CO_2$  molecule is expected to proceed *via* electron donation into the  $CO_2$   $\pi_u$  orbitals, thus bending the  $CO_2$  molecule,<sup>10</sup> two Kick runs were also undertaken explicitly searching for minima and transition states, employing the  $M_4$  cluster and a bent  $CO_2$  molecule as fragments. Additional starting geometries were generated by hand (*e.g.*  $CO_2$  bound to different symmetry-distinct metal atoms, end-on/side-on, linear/bent,  $\mu^1/\mu^2/\mu^3$ -bound). From these calculations, the physisorbed “capture” species and the  $M_4CO_2$  global minimum were identified, and the reaction pathway was then filled in and confirmed by a series of Quasi-Synchronous Transit (QST) and Intrinsic Reaction Coordinate (IRC) calculations. Where the global minimum was not a dissociated structure (*i.e.*  $M_4 + O + C + O$ ), the lowest energy dissociated structure was also identified and a pathway to that structure was calculated using QST and IRC calculations as above.

The zero energy for each  $M_4 + CO_2$  system is defined as the sum of the energies of the  $M_4$  metal cluster in the singlet

multiplicity and the  $CO_2$  molecule. Thus structures with a negative relative energy (below zero energy) are more stable than the separated reactants; structures with a positive relative energy (energy higher than zero energy) are unstable with respect to the infinitely separated reactants. As in a previous study, basis set superposition error (BSSE) was disregarded, as were zero-point energies and entropic contributions.<sup>39</sup> All structure searches (Kick runs) were undertaken with the B3P86 density functional<sup>40</sup> and Stuttgart Relativistic Small Core (SRSC) basis set,<sup>41-43</sup> as previous studies<sup>39,44</sup> have shown this to be an accurate and computationally efficient combination. The final pathways were re-optimized at all relevant multiplicities using the TPSS functional<sup>45</sup> with the Def2TZVP basis set<sup>46,47</sup> and employing the D3-BJ empirical dispersion term.<sup>48</sup> This latter combination, while more expensive, has also been shown to reproduce energetic ordering and vibrational data for reactions of small molecules on gas phase transition metal clusters including  $Rh_n$ <sup>49</sup> and  $Pt_n$ .<sup>50</sup> Gaussian 16 was used for all calculations.<sup>51</sup> Absolute and relative energies for all structures calculated with both functionals are presented in the SI (xlsx), structures are included in xyz format (zipfile).

## 3 Results and discussion

All  $M_4$  tetramers are even-electron species, and thus we calculate the singlet – septet surfaces by default.

### 3.1 $Nb_4$

For the  $Nb_4$  cluster we find a tetrahedral structure of singlet multiplicity to be the lowest in energy, in line with previous calculations using several DFT methods,<sup>52-55</sup> and confirmed by coupled cluster<sup>56</sup> and multireference singles and doubles configuration interaction (MRSDCI).<sup>57</sup> This cluster was used for the  $CO_2$  pathway without constraint.

The  $Nb_4 + CO_2$  pathway is shown in Fig. 1 and the corresponding geometric data is tabulated in Table S1. Only the singlet and triplet surfaces are shown as the quintet and septet were high in energy. The capture species (Fig. 1-I) is bound by  $-0.29$  eV and consists of the  $CO_2$  molecule approaching one vertex of the  $Nb_4$  tetrahedron. The  $CO_2$  molecule bends in the first transition state and the central carbon atom is  $\mu^2$  bound to a  $Nb-Nb$  edge, rotation of the  $CO_2$  molecule over a  $Nb_3$  face allows the first oxygen atom to dissociate (Fig. 1-V) and the remaining CO molecule dissociates the same way over the adjacent face resulting in a fully dissociated global minimum with a relative energy  $-6.61$  eV below zero energy.

### 3.2 $Mo_4$

Several groups have undertaken calculations on the  $Mo_4$  cluster: a recent DFT study by Kantorovich and coworkers predicted seven isomers within 1 eV of the global minimum, and two of those structures were separated by only 0.034 eV per atom – both structures were “tetrahedron-like” and possessed  $D_{2d}$  symmetry, but differed in the hinge angle.<sup>58</sup> Liebing *et al.* predict a stretched tetrahedral structure,<sup>59</sup> while Yin *et al.*



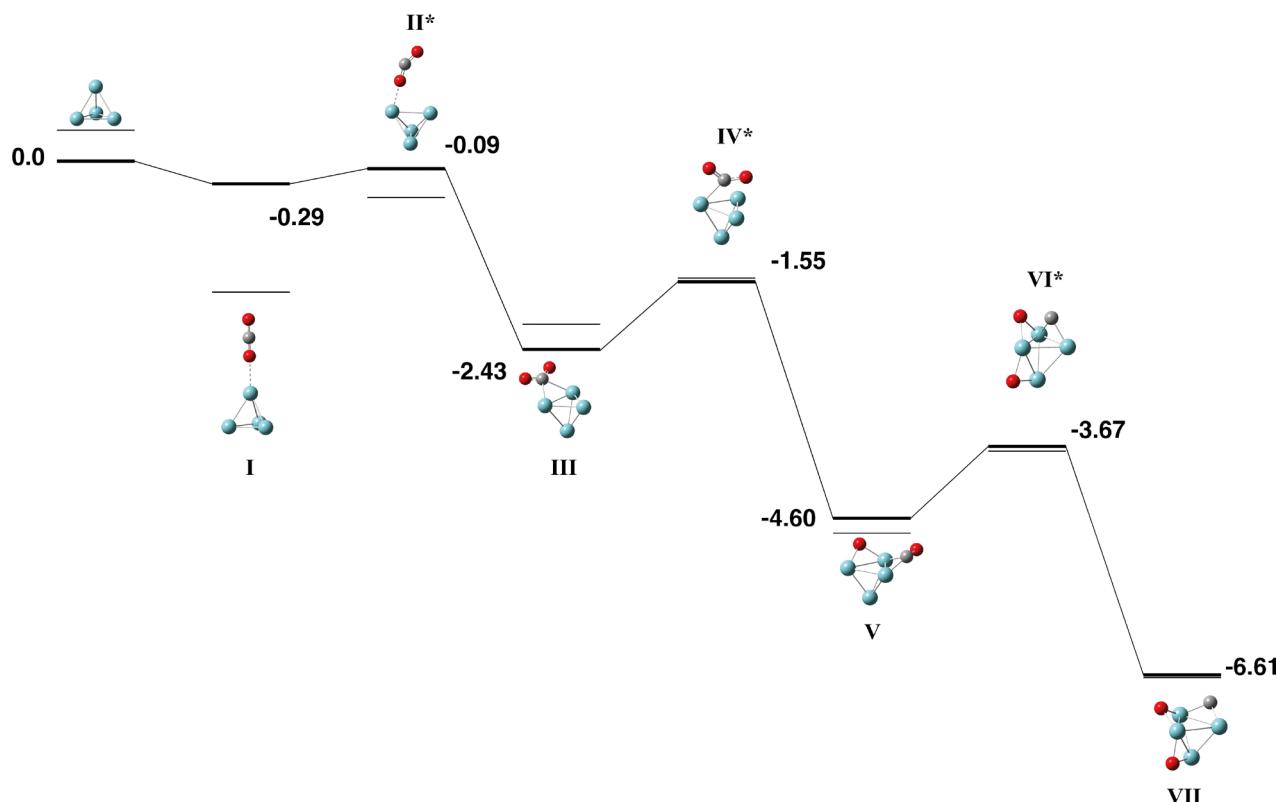


Fig. 1 Stationary points on the Nb<sub>4</sub> + CO<sub>2</sub> potential energy surface. The singlet multiplicity is shown in bold and the triplet multiplicity is shown with thin lines. Metal atoms are shown in blue/green, oxygen atoms are shown in red and the carbon atom is shown in grey.

predict a tetrahedral global minimum with an open “butterfly” structure 0.34 eV higher in energy.<sup>60</sup> Sumer and Jellinek reverse this order, predicting an open butterfly structure with  $\mu_B = 4$  being 0.01 eV per atom lower in energy than a tetrahedral structure with  $\mu_B = 2$ .<sup>61</sup> Pis Diez undertook a detailed study of the symmetry of the Mo<sub>4</sub> structure and identified four distorted tetrahedra of  $D_{2d}$  symmetry, a  $D_2$  structure and a  $C_{3v}$  triangular pyramid.<sup>62</sup> Our structure search on the singlet surface identified the open butterfly ( $\phi = 130^\circ$ ), stretched tetrahedron ( $\phi = 50^\circ$ ) and

tetrahedral structures and the open butterfly was employed as a fragment in the reaction path with CO<sub>2</sub>. It is to be noted, that despite starting from the open butterfly structure, upon interaction with CO<sub>2</sub>, the Mo<sub>4</sub> cluster became more compact, resembling either the tetrahedron or stretched tetrahedral structures.

The reaction path for Mo<sub>4</sub> + CO<sub>2</sub> is very similar to that of Nb<sub>4</sub> and is shown in Fig. 2 with the corresponding geometric data in Table S2. The singlet–quintet surfaces are shown as the septet surface is high in energy. The CO<sub>2</sub> molecule initially

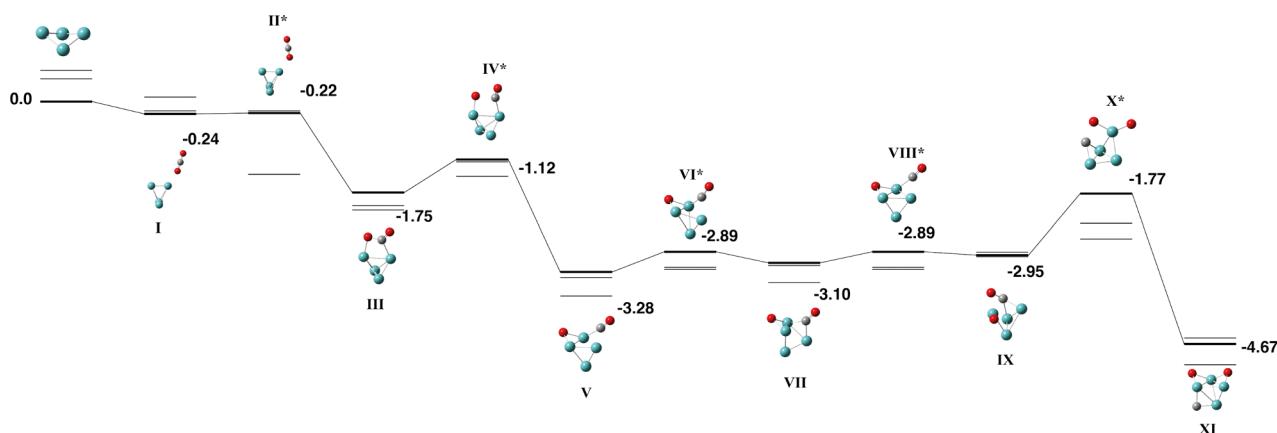


Fig. 2 Stationary points on the Mo<sub>4</sub> + CO<sub>2</sub> potential energy surface. The singlet multiplicity is shown in bold and the triplet–quintet multiplicities are shown with thin lines. Relative energies are given in eV. Metal atoms are shown in blue/green, oxygen atoms are shown in red and the carbon atom is shown in grey.



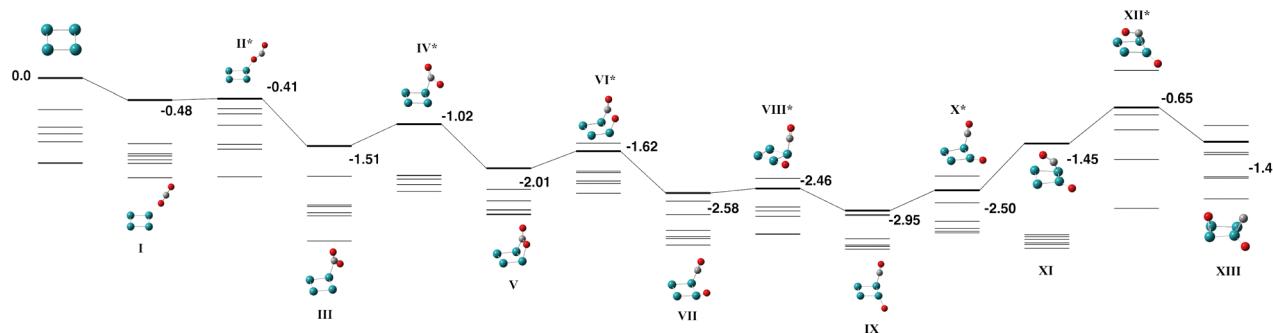


Fig. 3 Stationary points on the  $\text{Ru}_4 + \text{CO}_2$  potential energy surface. The singlet multiplicity is shown in bold and the triplet-13-tet multiplicities are shown with thin lines. Relative energies are given in eV. Metal atoms are shown in blue/green, oxygen atoms are shown in red and the carbon atom is shown in grey.

approaches a single Mo atom in the capture species before binding in a  $\eta^2$  fashion across a Mo–Mo bond (Fig. 2-III). The first O–CO bond breaks to yield a  $\mu^2$ -bound oxygen atom and a  $\mu^1$ -bound CO molecule (Fig. 2-V), which rotates to become  $\mu^2$ -bound (Fig. 2-VII) before dissociating. The lowest energy structure has  $\text{CO}_2$  fully dissociated and is  $-4.67$  eV below the energy of the separated  $\text{Mo}_4$  (singlet) and  $\text{CO}_2$ . The equivalent triplet structure is  $-5.07$  eV below zero energy.

### 3.3 $\text{Ru}_4$

As ruthenium is known to have low-lying states with a high number of unpaired electrons, multiplicities up to 15-tet are investigated for the  $\text{Ru}_4 + \text{CO}_2$  reaction. The lowest energy  $\text{Ru}_4$  structure was determined to be a singlet rectangle with side lengths of  $2.21$  and  $2.24$  Å which is in approximate agreement with previous calculations on the  $\text{Ru}_4$  cluster that predict a  $D_{4h}$  singlet square structure.<sup>63–65</sup>

Fig. 3 and Table S3 show the reaction path for  $\text{Ru}_4 + \text{CO}_2$ . Multiplicities up to the 13-tet are shown, the 15-tet was approximately 1 eV higher in energy throughout the entire pathway. The  $\text{CO}_2$  molecule interacts first with a single ruthenium atom in the capture species (Fig. 3-I), before bending and

rotating to form a Ru–C covalent bond (Fig. 3-III). On the singlet surface this step requires surmounting a barrier at  $+0.57$  eV, but for all other multiplicities, this transition state is below zero energy. The  $\text{CO}_2$  molecule rotates to locate one oxygen atom over the adjacent Ru atom, forming a  $\mu^2\eta^2$  structure. The lowest energy structure is Fig. 3-IX, where the  $\text{CO}_2$  molecule has partly dissociated to a  $\mu^1$ -bound oxygen atom in the  $\text{Ru}_4$  plane and a  $\mu^1$ -bound CO molecule approximately perpendicular to the plane. The remaining CO molecule can then fall across the  $\text{Ru}_4$  face and dissociate (Fig. 3-XIII), however, the dissociation of the second CO bond, while still below zero energy, is less favoured than the partly dissociated  $\text{CO}_2$  structure (Fig. 3-VII).

### 3.4 $\text{Rh}_4$

As with ruthenium, we consider additional multiplicities for the  $\text{Rh}_4$  cluster reaction, from singlet–nonet. The lowest energy  $\text{Rh}_4$  cluster was identified to be a singlet tetrahedron of  $T_d$  symmetry and a side length of  $2.45$  Å. This result is consistent with that of many authors<sup>66–70</sup> and we employ this structure, without constraint, as a fragment for reaction with  $\text{CO}_2$ .

Fig. 4 shows the reaction path for  $\text{Rh}_4 + \text{CO}_2$ , the corresponding geometric data is tabulated in Table S4. From the

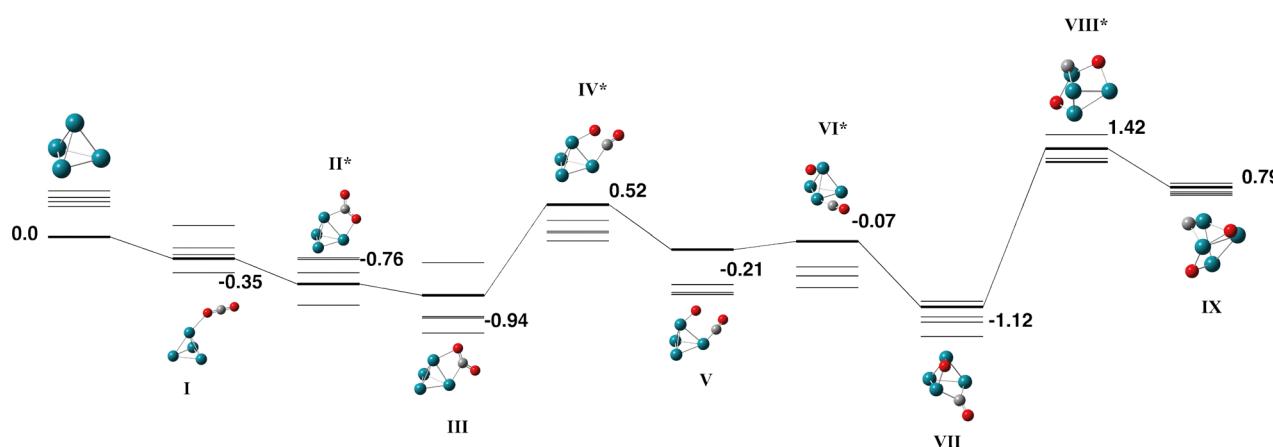


Fig. 4 Stationary points on the  $\text{Rh}_4 + \text{CO}_2$  potential energy surface. The singlet multiplicity is shown in bold and the triplet–nonet multiplicities are shown with thin lines. Relative energies are given in eV. Metal atoms are shown in blue/green, oxygen atoms are shown in red and the carbon atom is shown in grey.



$\eta^1$ -O bound capture species, the  $\text{CO}_2$  molecule falls across a Rh-Rh bond, binding in a  $\mu^2\eta^2$  fashion, with a O-C-O angle,  $\theta_{\text{OCO}} = 140^\circ$ , but only marginally lengthening the CO bond ( $r_{\text{CO}} = 1.26$  and  $1.27 \text{ \AA}$ ). The transition state stretching the coordinated CO bond ( $\nu_{\text{imag}} = 464 \text{ cm}^{-1}$ ) is  $+0.52 \text{ eV}$  higher than zero energy. After the first CO bond breaks, both the intact CO molecule and the dissociated oxygen atom rotate around the cluster, shifting from  $\mu^1$  to  $\mu^2$  binding in the lowest energy  $\text{Rh}_4\text{CO}_2$  cluster (Fig. 4-VII). To reach the lowest energy fully dissociated structure, Fig. 4-IX,  $+0.79 \text{ eV}$  above zero energy, the second CO bond needs to be stretched over an adjacent  $\text{Rh}_3$  face, surmounting a transition state of  $+1.42 \text{ eV}$ . Given that all transition states involving stretching of a CO bond have energy above that of the separated reactants, it is likely that  $\text{CO}_2$  would remain intact on the  $\text{Rh}_4$  cluster.

### 3.5 $\text{Pd}_4$

$\text{Pd}_4$  has also been extensively calculated. Futschek *et al.* calculated square, rhombus and tetrahedral structures with different multiplicities and point group symmetries, concluding that the triplet tetrahedron was the global minimum.<sup>67</sup> This assignment is in agreement with Kawazoe and coworkers<sup>71</sup> Moc *et al.* also employ a tetrahedral triplet ( ${}^3\text{A}'$ )  $\text{Pd}_4$  structure in their reaction with  $\text{H}_2$  molecules. Our structure search also identified a triplet global minimum, with a tetrahedral structure, though with a slightly expanded dihedral angle of  $74^\circ$  (*viz.*  $80^\circ$  in the singlet and  $70.5^\circ$  in  $T_d$  symmetry). We use this fragment going forward.

In addition to calculations determining the structure of the  $\text{Pd}_4$  cluster, there have been many DFT studies on reactions of  $\text{Pd}_4$ . Borbolla *et al.* in their B3LYP/6-31G(d,p) study, determined that the adsorption of formic acid on  $\text{Pd}_4$  would favourably produce  $\text{CO}_2$ .<sup>72</sup> Lian and coworkers showed that  $\text{Pd}_4^-$  had a lower barrier to dissociating  $\text{N}_2\text{O}$  than the neutral or cationic tetramers<sup>73</sup> and Dutta *et al.* compared the bare and ZSM-5-supported  $\text{Pd}_4$  cluster for the same reaction.<sup>74</sup> Kalita and Deka calculated reaction profiles for CO oxidation on bare and oxidized  $\text{Pd}_4$  clusters.<sup>75</sup>

The reaction path calculated for  $\text{Pd}_4 + \text{CO}_2$  is shown in Fig. 5 with geometric data in Table S5. The lowest energy species for

$\text{Pd}_4\text{CO}_2$  is Fig. 5-III, just after the capture species (Fig. 5-I). In structure Fig. 5-III, the  $\text{CO}_2$  molecule is bent over a  $\text{Pd-Pd}$  bond, with  $\theta_{\text{OCO}} = 136^\circ$  and  $r_{\text{CO}} = 1.24$  and  $1.30 \text{ \AA}$ . From this lowest energy structure, the  $\text{CO}_2$  molecule can rotate over the  $\text{Pd}_3$  face to form a  $\mu^3\eta^2$  geometry, which possesses approximate  $C_s$  symmetry, and a highly activated CO bond,  $r_{\text{CO}} = 1.36 \text{ \AA}$ . In transition state Fig. 5-VI, the activated CO bond breaks ( $\nu_{\text{imag}} = 261 \text{ cm}^{-1}$ ), but this barrier lies above zero energy at  $+0.28 \text{ eV}$ . Structure Fig. 5-VII is very similar to the  $\mu^2$ -O and  $\mu^2$ -CO structure calculated by Kalita and Deka for the coadsorption of  $\text{O}_2$  and CO on  $\text{Pd}_4$ .<sup>75</sup> Continuing the reaction path in order to dissociate the CO molecule is highly disfavoured, crossing a barrier of  $+3.42 \text{ eV}$  in order to reach a minimum  $+3.30 \text{ eV}$  higher in energy than the separated  $\text{Pd}_4 + \text{CO}_2$  reactants.

### 3.6 $\text{Pt}_4$

Our structure search identified a singlet open butterfly structure ( $\phi = 135^\circ$ ) as the global minimum structure. In contrast, Sebetci predicted a distorted tetrahedron ground state, followed by a butterfly structure, though these differed by only  $0.1 \text{ eV}$  per atom in binding energy.<sup>76</sup> Grönbeck and Andreoni reversed this prediction for the neutral  $\text{Pt}_4$  cluster, and additionally predicted a Y-shape cluster as being low in energy, further noting that the singlet and triplet states were quasi-degenerate.<sup>77</sup> The butterfly structure was also predicted by Singh *et al.*<sup>78</sup> and by Kawazoe and coworkers.<sup>79</sup> We employ our singlet butterfly as a fragment with  $\text{CO}_2$ .

Platinum is of long-standing interest and use as a catalyst. Of particular note, Mafuné and coworkers used DFT to show that small  $\text{Pt}_n$  ( $n = 4-12$ ) clusters could undergo oxygen transfer reactions with  $\text{N}_2\text{O}$  but did not catalyse the oxidation of CO, instead co-adsorbing O + CO.<sup>80</sup> Mass spectra generated in the same joint experimental – computational study were unable to identify  $\text{CO}_2$  desorption from the  $\text{Pt}_n$  clusters. In a later work, Green *et al.* predicted a dissociative (O + CO) global minimum for the reaction of the anionic  $\text{Pt}_4^-$  cluster, but infrared multiphoton dissociation (IR-MPD) showed that the  $\text{CO}_2$  molecule remained intact.<sup>35</sup>

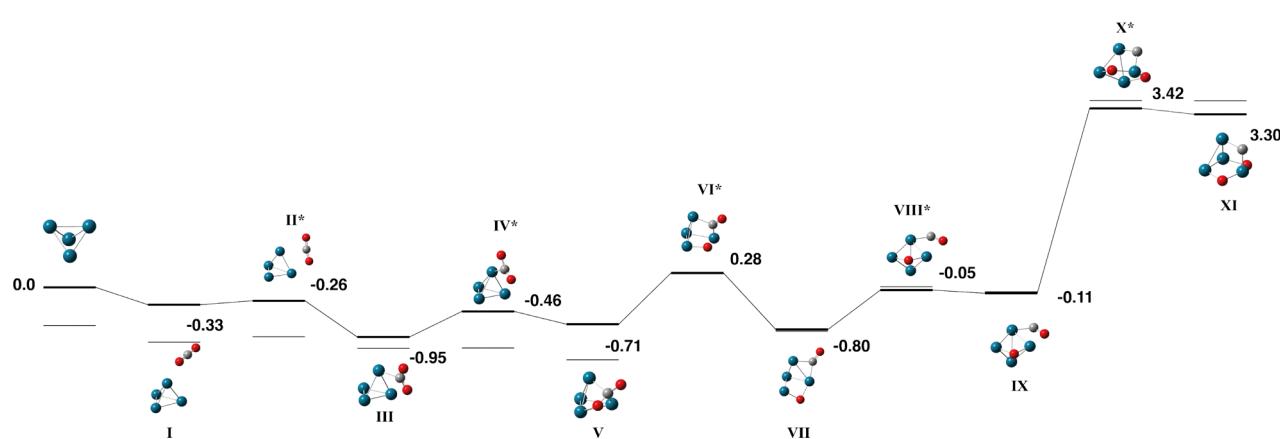


Fig. 5 Stationary points on the  $\text{Pd}_4 + \text{CO}_2$  potential energy surface. The singlet multiplicity is shown in bold and the triplet multiplicity is shown with thin lines. Relative energies are given in eV. Metal atoms are shown in blue/green, oxygen atoms are shown in red and the carbon atom is shown in grey.



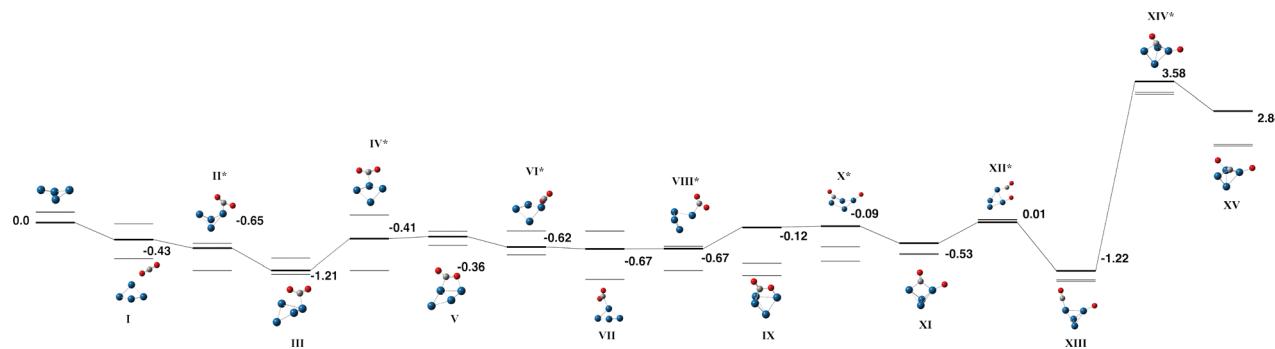


Fig. 6 Stationary points on the  $\text{Pt}_4 + \text{CO}_2$  potential energy surface. The singlet multiplicity is shown in bold and the triplet–quintet multiplicities are shown with thin lines. Relative energies are given in eV. Metal atoms are shown in blue/green, oxygen atoms are shown in red and the carbon atom is shown in grey.

The calculated reaction path for neutral  $\text{Pt}_4 + \text{CO}_2$  is shown in Fig. 6 with the corresponding data in Table S6. Green *et al.* noted that the anionic  $\text{Pt}_4^-$  cluster is a fluxional species,<sup>35</sup> and similar fluxionality is observed here for the neutral  $\text{Pt}_4$  cluster, which contracts from an open butterfly structure,  $\phi = 135^\circ$  for  $\text{Pt}_4$  to a tetrahedral structure,  $\phi = 76^\circ$  for the lowest energy structure Fig. 6-XIII. The key features on the reaction path are similar to those identified for the anionic cluster; after the capture species (Fig. 6-I), which is bound by  $-0.43$  eV, a C-bound  $\eta^1$  structure is formed (Fig. 6-III). The  $\text{CO}_2$  molecule may be  $\eta^1$ -bound in this way to either an apex (Fig. 6-III) or spinal atom (Fig. 6-VII) of the  $\text{Pt}_4$  butterfly, converting *via* an  $\eta^2$  CO binding across the Pt–Pt bond (Fig. 6-V). From Fig. 6-IX, the  $\text{CO}_2$  molecule could dissociate *via* either a opening/closing of the  $\text{Pt}_4$  cluster (Fig. 6-X) or *via* stretching of the OC bond (Fig. 6-XII). The lowest energy  $\text{Pt}_4\text{CO}_2$  structure has a  $\mu^1$ -bound CO molecule with the dissociated oxygen atom  $\mu^1$  bound to an adjacent Pt atom. Searching for a pathway to dissociate the intact CO molecule identified a transition state  $+3.58$  eV above

zero energy and a minimum  $+2.84$  eV above zero energy, indicating that full dissociation of the  $\text{CO}_2$  molecule to  $\text{O} + \text{C} + \text{O}$  is not thermodynamically feasible on the  $\text{Pt}_4$  cluster.

### 3.7 $\text{Ag}_4$

Silver has an electronic configuration of  $4\text{d}^{10}5\text{s}^1$ , and we study the singlet–septet multiplicities. The global minimum  $\text{Ag}_4$  structure is predicted to be a planar singlet rhombus structure of  $D_{2h}$  symmetry, in agreement with several previous calculations.<sup>81–84</sup> Attempts to converge a tetrahedral structure, similar to the  $\text{Ag}_4^{2+}$  structure calculated by Shimizu and coworkers, resulted in a stretched tetrahedron 0.95 eV higher in energy.<sup>85</sup> A recent study indicated that the diamond/rhombus structure of  $\text{Ag}_4$  contributed strongly to the activation of  $\text{O}_2$ .<sup>86</sup>

The global minimum planar rhombus  $\text{Ag}_4$  structure was used as the basis for the reaction path finding and the resulting  $\text{Ag}_4 + \text{CO}_2$  reaction path is shown in Fig. 7 and Table S7. Only the singlet surface is shown as all other multiplicities were significantly above zero energy.  $\text{CO}_2$  interacts only weakly with

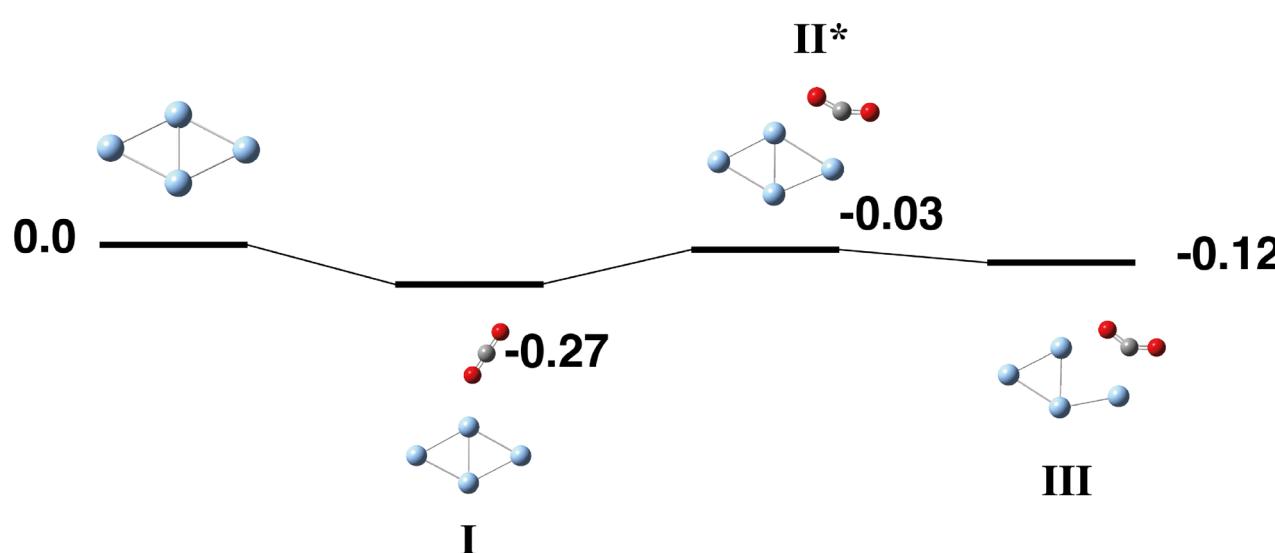


Fig. 7 Stationary points on the  $\text{Ag}_4 + \text{CO}_2$  potential energy surface. The singlet multiplicity is shown with bold lines. Other multiplicities are high in energy and are not shown. Relative energies are given in eV. Metal atoms are shown in blue/green, oxygen atoms are shown in red and the carbon atom is shown in grey.



the  $\text{Ag}_4$  cluster, the capture species (Fig. 7-I) has  $\text{CO}_2$   $\mu^1$ -bound to a spinal  $\text{Ag}$  atom. The  $\text{CO}_2$  molecule could then rotate in the  $\text{Ag}_4$  plane and bend to form a  $\mu^2\eta^2$  structure, but at the expense of the  $\text{Ag}-\text{Ag}$  bond, which is broken ( $3.79 \text{ \AA}$  vs.  $2.76 \text{ \AA}$ ). In Fig. 7-III,  $r(\text{Ag}-\text{C})$  and  $r(\text{Ag}-\text{O})$  are  $2.23$  and  $2.24 \text{ \AA}$  respectively. No structures with  $\text{CO}_2$  either partly ( $\text{O} + \text{CO}$ ) or fully ( $\text{O} + \text{C} + \text{O}$ ) dissociated were obtained.

### 3.8 Periodic trends

For each  $\text{M}_4 + \text{CO}_2$  reaction path, several key species are identified, these are: (1) the capture species, which is always the first structure shown on each reaction path and represents the first (physisorption) interaction between  $\text{CO}_2$  with the  $\text{M}_4$  cluster, the  $\text{CO}_2$  molecule is therefore still linear in the capture species. (2) The lowest energy species with associatively-bound  $\text{CO}_2$ , the  $\text{CO}_2$  molecule is, by definition, intact, but may not be linear. This species represents an activated  $\text{CO}_2$  molecule. If a stable activated  $\text{CO}_2$  molecule could be thermodynamically or kinetically prevented from further activation  $\rightarrow$  dissociation (to  $\text{O} + \text{CO}$ ), the activated  $\text{CO}_2$  might thus be available for reaction with *e.g.*  $\text{H}_2$  to form formaldehyde. (3) The lowest energy structure with one  $\text{CO}$  bond broken, *i.e.*  $\text{M}_4\text{O}\cdot\text{CO}$ . (4) The lowest energy structure with the  $\text{CO}_2$  fully dissociated to atoms. In the context of  $\text{CO}_2$  activation, this would represent a catalyst poisoning process. The relative energies of these four geometric motifs are shown in Fig. 8.

The energy of the capture species is consistent across the periodic table, ranging from  $-0.23 \text{ eV}$  ( $\text{Mo}_4$ ) up to  $-0.48 \text{ eV}$  for the square planar  $\text{Ru}_4$  cluster. The consistency of this interaction is expected, given the definition of the capture species as the minimally interacting species and has been observed previously.<sup>39</sup> The relative energies of the associative ( $\text{OCO}$ ), partly dissociated ( $\text{O} + \text{CO}$ ) and fully dissociated ( $\text{O} + \text{C} + \text{O}$ ) structures steadily increasing as one moves left to right across the periodic table, from  $\text{Nb}_4$  to  $\text{Ag}_4$ . Note that no structures with dissociatively bound  $\text{CO}_2$  were identified for  $\text{Ag}_4$ . The apparent 'slope' of energy increase, is mild for associative structures, moderate in the case of partly dissociated structures ( $\text{O} + \text{CO}$ ) and strong for the fully dissociated structures. Fully dissociated structures are disfavoured (higher than zero energy) for  $\text{Rh}_4$ ,  $\text{Pd}_4$  and  $\text{Pt}_4$ . The energies for the third row  $\text{Pt}_4$  cluster are similar, but slightly lower than the equivalent  $\text{Pd}_4\text{CO}_2$  structures, suggesting that small clusters to the right of (and including) rhodium, would not fully dissociate  $\text{CO}_2$ .

The initial adsorption step is considered key to the activation of  $\text{CO}_2$ ,<sup>87</sup> it is the first step where charge transfer from the cluster to the  $\text{CO}_2$  molecule, typically *via* the electrophilic carbon atom occurs, weakening the  $\text{C}=\text{O}$  bonds, bending  $\theta_{\text{OCO}}$  and thereby leading to a variety of stable intermediate structures.<sup>87</sup> We therefore consider the properties of the  $\text{M}_4\text{CO}_2$  capture species for each reaction pathway: Table 1 shows the calculated vibrational frequencies of  $\text{CO}_2$  in the capture species for each  $\text{M}_4$  cluster. The two bending frequencies, now non-degenerate, are strongly red-shifted on interaction with the  $\text{M}_4$  cluster, by  $\approx 60 \text{ cm}^{-1}$ , consistent with the  $\text{CO}_2 \pi_u$  antibonding orbitals receiving electron density from the

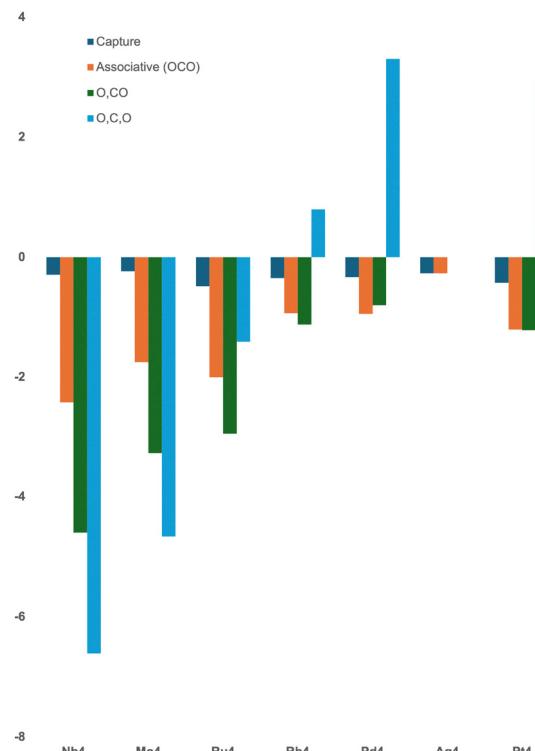


Fig. 8 Plot of the relative energies of capture, lowest energy associative ( $\text{OCO}$ ), lowest energy partly dissociated ( $\text{O},\text{CO}$ ) and fully dissociative ( $\text{O},\text{C},\text{O}$ ) structures of  $\text{M}_4$  metal clusters in the singlet multiplicity.

cluster. Considering the first of the two formerly degenerate frequencies (the one with the larger redshift), there is an apparent, though approximate, correlation between the degree of redshift and the energy of the fully dissociative species, with clusters that possess a fully dissociated  $\text{CO}_2$  below zero energy, regardless of whether this structure is the global minimum or not, show a redshift  $> 60 \text{ cm}^{-1}$  (*viz.*  $\text{Nb}_4$ ,  $\text{Mo}_4$  and  $\text{Ru}_4$ ). Clusters to the right of and including  $\text{Rh}_4$  yield a smaller redshift.

Table 1 also shows the energy of the  $\text{CO}_2 \pi_u$  orbital and the  $\Delta E$ , with respect to the calculated value for free  $\text{CO}_2$  ( $-0.03280 \text{ a.u.}$ ). Clusters that thermodynamically dissociate  $\text{CO}_2$  lower the energy of the  $\pi_u$  orbital by  $\approx 1.2\text{--}1.5 \text{ eV}$ , while clusters without a fully dissociated  $\text{CO}_2$  below zero energy, lower the orbital energy by only  $\approx 0.5\text{--}0.9 \text{ eV}$ . Both of these correlations are indicative only, and provide no information on the relative stability of intermediate species (*e.g.*  $\text{M}_4\text{O}\cdot\text{CO}$ ) but do act as a barometer for the thermodynamic stability (below zero energy) of the fully dissociative structure.

Table 1 shows the properties of the capture species for each reaction pathway, defined previously as the initial contact of  $\text{CO}_2$  with the metal cluster. As this species possesses  $\text{CO}_2$  physisorbed to the  $\text{M}_4$  cluster, the interaction of the two species is minimal, and it is perhaps unsurprising that consideration of this species alone is insufficient to predict the eventual fate of  $\text{CO}_2$ . Table 2 shows the Hirshfeld charges on  $\text{CO}_2$  molecule in the capture species and the first transition state for each of the reaction pathways.  $q(\text{CO}_2)$  for the capture species is consistent



**Table 1**  $\text{CO}_2$  vibrational frequencies ( $\nu_{\text{CO}_2}$ ), key orbital energies and adsorption and interaction energies for  $\text{M}_4\text{CO}_2$  capture species. Absolute energy of the  $\text{CO}_2 \pi_u$  orbital is  $-0.893$  eV ( $-0.03280$  a.u)

System	Bend 1	Bend 2	Symm stretch	Asym stretch	$E(\text{M}_4, \text{HOMO})$	$E(\text{M}_4, \text{LUMO})$	$E(\pi_u)$	$\Delta E(\pi_u)$	$E_{\text{ads}}$	$E_{\text{int}}$
	(cm <sup>-1</sup> )				(eV)					
$\text{CO}_2$	622	622	1283	2319			$-0.893$	0.0		
$\text{Nb}_4$	546	547	1256	2317	-4.237	-2.304	-2.304	-1.411	-0.291	-0.292
$\text{Mo}_4$	471	540	1251	2333	-3.920	-2.399	-2.399	-1.507	-0.237	-0.516
$\text{Ru}_4$	527	579	1268	2324	-4.905	-3.470	-2.140	-1.248	-0.481	0.514
$\text{Rh}_4$	572	587	1275	2322	-5.416	-3.000	-1.393	-0.501	-0.349	-0.351
$\text{Pd}_4$	581	585	1277	2322	-5.495	-4.245	-1.498	-0.605	-0.333	-0.341
$\text{Ag}_4$	599	606	1292	2331	-5.232	-3.130	-1.822	-0.930	-0.269	-0.269
$\text{Pt}_4$	567	588	1280	2330	-6.060	-4.227	-1.797	-0.904	-0.430	-0.433

**Table 2** Hirshfeld charge on  $\text{CO}_2$  in capture species and first transition state for  $\text{M}_4\text{CO}_2$  reaction pathways

System	Capture species		TS 1
	$q(\text{CO}_2)$	$q(\text{CO}_2)$	
$\text{Nb}_4$	0.098		-0.577
$\text{Mo}_4$	0.097		-0.488
$\text{Ru}_4$	0.125		-0.354
$\text{Rh}_4$	0.097		-0.299
$\text{Pd}_4$	0.080		-0.006
$\text{Ag}_4$	0.087		-0.151
$\text{Pt}_4$	0.114		-0.250

and positive ( $\approx 0.1$ ) for all  $\text{M}_4$  clusters, and clearly represents the initial donation of charge from the  $\text{CO}_2$  molecule to the cluster. The charge transfer observed in the first transition state (*i.e.* the back-donation from the  $\text{M}_4$  cluster to the  $\text{CO}_2$  molecule upon chemisorption) is diagnostic, with the three species where full  $\text{CO}_2$  dissociation is thermodynamically possible (*viz.*  $\text{Nb}_4$ ,  $\text{Mo}_4$  and  $\text{Ru}_4$ ) having  $q(\text{CO}_2) < -0.35e^-$ . Clusters that do not dissociate either  $\text{CO}_2$  bond, ( $\text{Pd}_4$  and  $\text{Ag}_4$ ) have low back-donation to  $\text{CO}_2$ ,  $< 0.2e^-$  and clusters that are likely to activate  $\text{CO}_2$  without fully dissociating it,  $\text{Rh}_4$ ,  $\text{Pt}_4$ , having intermediate  $q(\text{CO}_2)$  values.

Fig. 9 shows the barrier heights (transition state energies) for the key transition states in each pathway. The chosen

barriers correspond to each CO bond breaking. Accordingly, no barriers are plotted for  $\text{Ag}_4$ . Two trends can be clearly observed. Firstly, there is a clear left-right divide with all  $\text{Nb}_4$ – $\text{Ru}_4$  barriers being below zero energy, whereas  $\text{Rh}_4$ – $\text{Pd}_4$  barriers are above zero energy. The barrier to breaking the first CO bond on  $\text{Pt}_4$  is slightly below zero energy at  $-0.12$  eV, reflecting the softer surface presented by the 5d metal compared to its 4d counterpart. Secondly, the barriers to the first CO bond breaking are relatively consistent either side of the left-right divide defined by  $\text{Ru}/\text{Rh}$ , whereas the barrier to the second CO bond breaking rises when moving from left to right ( $\text{Nb}_4$ – $\text{Ag}_4$ ), suggesting that activated  $\text{CO}_2$  or  $\text{O} + \text{CO}$  are likely outcomes of reaction on the  $\text{Rh}_4$  and  $\text{Pd}_4$  clusters.

The general trends in adsorption energies shown in Fig. 8 are consistent with other materials proposed for  $\text{CO}_2$  adsorption. Peng and coworkers studied the adsorption of molecular  $\text{CO}_2$  on  $\text{M}_2\text{N}$  MXenes, and found that end-on  $\text{CO}_2$  binding had a consistent binding energy, of  $\approx -0.25$  eV, corresponding to a physisorbed geometry, but the adsorption energy of side-on  $\text{CO}_2$  rose from  $-2.5$  eV for  $\text{Y}_2\text{N}$  to  $-1.5$  eV for  $\text{Mo}_2\text{N}$ , and MXenes to the right of  $\text{Ru}_2\text{N}$  bound  $\text{CO}_2$  only weakly,  $\approx -0.42$  eV. Jurado *et al.* also studied a range of  $\text{M}_2\text{X}$  MXenes, finding similar binding energies and trends with  $\text{CO}_2$  adsorption energies of  $-2.83$ ,  $-1.73$  and  $-1.34$  eV for  $\text{M} = \text{Zr}$ ,  $\text{Nb}$  and  $\text{Mo}$  respectively. In addition, they also noted the non-negligible role of the X atom, with carbides having lower adsorption energies than equivalent nitrides, and  $\text{M}_3\text{N}_2$  MXenes having adsorption energies  $\approx 1$  eV greater than the equivalent  $\text{M}_2\text{N}$  species. A study on single-atom doped  $\text{Ti}_2\text{CO}_2$  showed that  $\text{CO}_2$  remains intact on these species, which is consistent with the  $\text{CO}_2$  adsorption energy on Y-doped  $\text{Ti}_2\text{CO}_2$  of  $-0.808$  eV,<sup>88</sup> compared to  $\approx 2$  eV for the  $\text{M}_4$  species that dissociate  $\text{CO}_2$  in this work.

## 4 Conclusions

We have calculated reaction pathways for the reaction of  $\text{CO}_2$  on a series of neutral  $\text{M}_4$  transition metal clusters. Moving from left to right across the periodic table, the energies of the capture species remained relatively constant. The energies of the lowest energy  $\text{M}_4\text{CO}_2$  species with  $\text{CO}_2$  fully intact (associatively bound  $\text{CO}_2$ ), lowest energy  $\text{M}_4\text{O}-\text{CO}$  species and  $\text{M}_4\text{O}-\text{C-O}$  (fully dissociated  $\text{CO}_2$ ) species all rose moving from  $\text{Nb}_4$  to  $\text{Ag}_4$ , with the rate of increase  $\text{M}_4\text{O}-\text{C-O} > \text{M}_4\text{O}-\text{CO} > \text{M}_4\text{CO}_2$ . Therefore it is

**Fig. 9** Plot of the relative energies of barriers to dissociation of the first (blue) and second (orange) C–O bonds for  $\text{M}_4\text{CO}_2$  reaction pathways on the singlet surface.

predicted that  $\text{Nb}_4$  and  $\text{Mo}_4$  will fully dissociate  $\text{CO}_2$ .  $\text{Ru}_4$  may also fully dissociate  $\text{CO}_2$ , but would be more likely to only break the first CO bond, resulting in a  $\text{Ru}_4\text{O}\text{-CO}$  product.  $\text{Rh}_4$ ,  $\text{Pd}_4$  and  $\text{Pt}_4$  are good candidates to observe an activated  $\text{CO}_2$  molecule. The  $\text{Ag}_4$  cluster interacts only weakly with  $\text{CO}_2$ . The energy of the  $\text{CO}_2 \pi_u$  orbital in the  $\text{M}_4\text{CO}_2$  capture species and the related  $\nu_{\text{bend}}$  was found to indicate those structures that dissociate  $\text{CO}_2$  fully ( $\text{Nb}_4$ ,  $\text{Mo}_4$  and  $\text{Ru}_4$ ) from those that do not, but did not distinguish between partly dissociated ( $\text{O} + \text{CO}$ ) and fully intact  $\text{CO}_2$ , however the degree of charge transfer in the first transition state was found to indicate all three possible fates of  $\text{CO}_2$ .

## Author contributions

SS, BAV, NA, MS: investigation, writing – original draft MAA: conceptualization of this study, methodology, writing – review and editing.

## Conflicts of interest

There are no conflicts to declare.

## Data availability

The data supporting this article have been included as part of the supplementary information (SI). Supplementary information: geometric parameters (pdf), structures (xyz) and energies, vibrational data (xlsx) for all pathways. See DOI: <https://doi.org/10.1039/d5cp03419a>.

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## Notes and references

- 1 G. A. Olah, G. K. S. Prakash and A. Goeppert, *J. Am. Chem. Soc.*, 2011, **133**, 12881–12898.
- 2 E. V. Kondratenko, G. Mul, J. Baltrusaitis, G. O. Larrazábal and J. Pérez-Ramírez, *Energy Environ. Sci.*, 2013, **6**, 3112–3135.
- 3 R. W. Dorner, D. R. Hardy, F. W. Williams and H. D. Willauer, *Energy Environ. Sci.*, 2010, **3**, 884–890.
- 4 A. G. Saputro, A. L. Maulana, F. D. Aprilyanti and H. K. Diponoro, *J. Eng. Technol. Sci.*, 2021, **53**, 210402.
- 5 V. K. Ocampo-Restrepo, L. G. Verga and J. L. F. Da Silva, *J. Phys. Chem. C*, 2021, **125**, 26296–26306.
- 6 X. Li, J. Yu, M. Jaroniec and X. Chen, *Chem. Rev.*, 2019, **119**, 3962–4179.
- 7 T. Sakakura, J.-C. Choi and H. Yasuda, *Chem. Rev.*, 2007, **107**, 2365–2387.
- 8 V. K. Ocampo-Restrepo, L. G. Verga and J. L. F. Da Silva, *J. Phys. Chem. C*, 2021, **125**, 26296–26306.
- 9 V. K. Ocampo-Restrepo, L. Zibordi-Besse and J. L. F. Da Silva, *J. Chem. Phys.*, 2019, **151**, 214301.
- 10 J. M. Weber, *Int. Rev. Phys. Chem.*, 2014, **33**, 489–519.
- 11 M. C. Thompson, J. Ramsay and J. M. Weber, *J. Phys. Chem. A*, 2017, **121**, 7534–7542.
- 12 C. Wu, M. Luo, Y. Zhao, S. Wang, A. Zavabeti, P. Xiao and G. K. Li, *Chem. Eng. J.*, 2023, **475**, 146411.
- 13 Q. Sun, S. Huang, Z. Li, D. Su and J. Sun, *J. Environ. Chem. Eng.*, 2023, **11**, 109065.
- 14 M. Zhang, D. Zhang, X. Jing, B. Xu and C. Duan, *Angew. Chem., Int. Ed.*, 2024, **63**, e202402755.
- 15 P. Du, G. Deng, Z. Li, J. Sun, L. Wang, Y. Yang, J. Wang, Y. Li, X. Xu, Y. Zhang, W. Liu, G. Liu, Z. Zou and Z. Li, *J. Mater. Sci. Technol.*, 2024, **189**, 203–210.
- 16 Y. Wang, Y. S. Chan, R. Zhang and B. Yan, *Chem. Eng. J.*, 2024, **481**, 148360.
- 17 O. Hurtado-Aular, R. M. Ferullo and P. G. Belelli, *Comput. Mater. Sci.*, 2024, **233**, 112741.
- 18 Y. Shao, S. Zhang, X. Ou, F. Zeng, R. Cai, X. Fan and H. Chen, *Chem. Eng. J.*, 2025, **518**, 164589.
- 19 D. Y. Shin, J. H. Jo, J.-Y. Lee and D.-H. Lim, *Comput. Theor. Chem.*, 2016, **1083**, 31–37.
- 20 H. Sugiyama, M. Miyazaki, M. Sasase, M. Kitano and H. Hosono, *J. Am. Chem. Soc.*, 2023, **145**, 9410–9416.
- 21 V. Muman, A. Tennyson-Davies, O. Allegret and M. A. Addicoat, *Phys. Chem. Chem. Phys.*, 2024, **26**, 2218–2227.
- 22 M. A. Addicoat, K. F. Lim and G. F. Metha, *J. Chem. Phys.*, 2012, **137**, 034301.
- 23 A. Fielicke, *Chem. Soc. Rev.*, 2023, **52**, 3778–3841.
- 24 A. Yamada, K. Miyajima and F. Mafune, *Phys. Chem. Chem. Phys.*, 2012, **14**, 4188–4195.
- 25 D. Harding, M. S. Ford, T. R. Walsh and S. R. Mackenzie, *Phys. Chem. Chem. Phys.*, 2007, **9**, 2130–2136.
- 26 S. Nayak, B. Rao, S. Khanna and P. Jena, *Chem. Phys. Lett.*, 1996, **259**, 588–592.
- 27 G. Kwon, G. A. Ferguson, C. J. Heard, E. C. Tyo, C. Yin, J. DeBartolo, S. Seifert, R. E. Winans, A. J. Kropf, J. Greeley, R. L. Johnston, L. A. Curtiss, M. J. Pellin and S. Vajda, *ACS Nano*, 2013, **7**, 5808–5817.
- 28 R. K. Raju, P. Rodriguez and E. N. Brothers, *Phys. Chem. Chem. Phys.*, 2023, **25**, 11630–11652.
- 29 K. Mori, J. Matsuo, Y. Kondo, H. Hata and H. Yamashita, *ACS Appl. Energy Mater.*, 2021, **4**, 11634–11642.
- 30 S. H. Pulumati, D. K. Sannes, C. R. Jabbour, L. D. B. Mandemaker, B. M. Weckhuysen, U. Olsbye, A. Nova and E. Skulason, *ACS Catal.*, 2023, **14**, 382–394.
- 31 M. N. Collacique, V. K. Ocampo-Restrepo and J. L. F. Da Silva, *J. Chem. Phys.*, 2022, **156**, 124106.
- 32 D. Guo, J. Liu, X. Zhao, X. Yang and X. Chen, *Sep. Purif. Technol.*, 2023, **313**, 123462.
- 33 J. Li, P. Gonzalez-Navarrete, M. Schlangen and H. Schwarz, *Chem. – Eur. J.*, 2015, **21**, 7780–7789.
- 34 M. A. Nolen, S. A. Tacey, S. Kwon and C. A. Farberow, *Appl. Surf. Sci.*, 2023, **637**, 157873.
- 35 A. E. Green, J. Justen, W. Schöllkopf, A. S. Gentleman, A. Fielicke and S. R. Mackenzie, *Angew. Chem., Int. Ed.*, 2018, **57**, 14822–14826.
- 36 U. Mondal and P. Ghosh, *Catal. Today*, 2021, **370**, 93–103.



37 M. A. Addicoat and G. F. Metha, *J. Comput. Chem.*, 2009, **30**, 57–64.

38 M. A. Addicoat, S. Fukuoka, A. J. Page and S. Irle, *J. Comput. Chem.*, 2013, **34**, 2591–2600.

39 M. A. Addicoat, M. A. Buntine, B. Yates and G. F. Metha, *J. Comput. Chem.*, 2008, **29**, 1497–1506.

40 A. D. Becke, *J. Chem. Phys.*, 1993, **98**, 5648–5652.

41 P. J. Hay and W. R. Wadt, *J. Chem. Phys.*, 1985, **82**, 270–283.

42 W. R. Wadt and P. J. Hay, *J. Chem. Phys.*, 1985, **82**, 284–298.

43 P. J. Hay and W. R. Wadt, *J. Chem. Phys.*, 1985, **82**, 299–310.

44 M. A. Addicoat, K. F. Lim and G. F. Metha, *J. Chem. Phys.*, 2012, **137**, 034301.

45 J. Tao, J. P. Perdew, V. N. Staroverov and G. E. Scuseria, *Phys. Rev. Lett.*, 2003, **91**, 146401.

46 F. Weigend and R. Ahlrichs, *Phys. Chem. Chem. Phys.*, 2005, **7**, 3297–3305.

47 F. Weigend, *Phys. Chem. Chem. Phys.*, 2006, **8**, 1057–1065.

48 S. Grimme, S. Ehrlich and L. Goerigk, *J. Comput. Chem.*, 2011, **32**, 1456–1465.

49 E. M. Cunningham, A. S. Gentleman, P. W. Beardsmore and S. R. Mackenzie, *Phys. Chem. Chem. Phys.*, 2019, **21**, 13959–13967.

50 G. Meizyte, A. E. Green, A. S. Gentleman, S. Schaller, W. Schöllkopf, A. Fielicke and S. R. Mackenzie, *Phys. Chem. Chem. Phys.*, 2020, **22**, 18606–18613.

51 M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, G. Scalmani, V. Barone, G. A. Petersson, H. Nakatsuji, X. Li, M. Caricato, A. V. Marenich, J. Bloino, B. G. Janesko, R. Gomperts, B. Mennucci, H. P. Hratchian, J. V. Ortiz, A. F. Izmaylov, J. L. Sonnenberg, D. Williams-Young, F. Ding, F. Lipparini, F. Egidi, J. Goings, B. Peng, A. Petrone, T. Henderson, D. Ranasinghe, V. G. Zakrzewski, J. Gao, N. Rega, G. Zheng, W. Liang, M. Hada, M. Ehara, K. Toyota, R. Fukuda, J. Hasegawa, M. Ishida, T. Nakajima, Y. Honda, O. Kitao, H. Nakai, T. Vreven, K. Throssell, J. A. Montgomery, Jr., J. E. Peralta, F. Ogliaro, M. J. Bearpark, J. J. Heyd, E. N. Brothers, K. N. Kudin, V. N. Staroverov, T. A. Keith, R. Kobayashi, J. Normand, K. Raghavachari, A. P. Rendell, J. C. Burant, S. S. Iyengar, J. Tomasi, M. Cossi, J. M. Millam, M. Klene, C. Adamo, R. Cammi, J. W. Ochterski, R. L. Martin, K. Morokuma, O. Farkas, J. B. Foresman and D. J. Fox, *Gaussian~16 Revision B.01*, Gaussian Inc., Wallingford CT, 2016.

52 X. X. Jin, J. G. Du, G. Jiang, X. Luo and X. W. Wang, *Eur. Phys. J. D*, 2011, **64**, 323–329.

53 P. V. Nhat, V. T. Ngan and M. T. Nguyen, *J. Phys. Chem. C*, 2010, **114**, 13210–13218.

54 P. Calaminici and R. Mejia-Olvera, *J. Phys. Chem. C*, 2011, **115**, 11891–11897.

55 X. Wang, M. Lin and Q. Zhang, *Acta Chim. Sin.*, 2004, **62**, 1689–1694.

56 C. V. S. Costa, L. d S. Barbosa, R. Gargano and D. L. Azevedo, *J. Mol. Mod.*, 2024, **30**, 406.

57 D. Majumdar and K. Balasubramanian, *J. Chem. Phys.*, 2004, **121**, 4014–4032.

58 Y. Wei, V. Veryazov and L. Kantorovich, *APL Mater.*, 2024, **12**, 031127.

59 S. Liebing, C. Martin, K. Trepte and J. Kortus, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2015, **91**, 155421.

60 Y.-H. Yin and J. Chen, *Comput. Theor. Chem.*, 2022, **1212**, 113720.

61 A. Sumer and J. Jellinek, *J. Chem. Phys.*, 2022, **157**, 034301.

62 R. Pis Diez, *Int. J. Quantum Chem.*, 2000, **76**, 105–112.

63 G.-X. Ge, H.-X. Yan, Q. Jing and Y.-H. Luo, *J. Cluster Sci.*, 2011, **22**, 473–489.

64 Y.-C. Bae, H. Osanai, V. Kumar and Y. Kawazoe, *Mater. Trans.*, 2005, **46**, 159–162.

65 F. Aguilera-Granja, L. C. Balbás and A. Vega, *J. Phys. Chem. A*, 2009, **113**, 13483–13491.

66 B. V. Reddy, S. K. Nayak, S. N. Khanna, B. K. Rao and P. Jena, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1999, **59**, 5214–5222.

67 T. Futschek, M. Marsman and J. Hafner, *J. Phys.: Condens. Matter*, 2005, **17**, 5927.

68 C.-H. Chien, E. Blaisten-Barojas and M. R. Pederson, *Phys. Rev. A: At., Mol., Opt. Phys.*, 1998, **58**, 2196–2202.

69 S. K. Nayak, S. E. Weber, P. Jena, K. Wildberger, R. Zeller, P. H. Dederichs, V. S. Stepnyuk and W. Hergert, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1997, **56**, 8849–8854.

70 Y. Jinlong, F. Toigo and W. Kelin, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1994, **50**, 7915–7924.

71 V. Kumar and Y. Kawazoe, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2002, **66**, 144413.

72 R. L. Camacho-Mendoza and J. Cruz-Borbolla, *Chem. Phys. Lett.*, 2020, **755**, 137794.

73 X. Tang, W. Zeng, H. Duan, S. Chen and X. Lian, *React. Kinet., Mech. Catal.*, 2023, **136**, 1933–1943.

74 P. Dutta, N. Biswakarma, D. Dowerah, S. Neog, A. Phonglo, P. J. Sarma, N. K. Gour and R. C. Deka, *J. Phys. Chem. C*, 2024, **128**, 21263–21279.

75 B. Kalita and R. C. Deka, *J. Am. Chem. Soc.*, 2009, **131**, 13252–13254.

76 A. Sebetci, *J. Chem. Phys.*, 2006, **331**, 9–18.

77 H. Grönbeck and W. Andreoni, *Chem. Phys.*, 2000, **262**, 1–14.

78 N. B. Singh and U. Sarkar, *J. Mol. Mod.*, 2014, **20**, 2537.

79 V. Kumar and Y. Kawazoe, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2008, **77**, 205418.

80 H. Yamamoto, K. Miyajima, T. Yasuike and F. Mafuné, *J. Phys. Chem. A*, 2013, **117**, 12175–12183.

81 N. Hartmann, R. Mitric, B. Stanca and V. Bonacic-Koutecky, *Eur. Phys. J. D*, 2001, **16**, 151–155.

82 V. Bonačić-Koutecky, L. Češpiva, P. Fantucci and J. Koutecky, *J. Chem. Phys.*, 1993, **98**, 7981–7994.

83 Y. Wang and X. G. Gong, *Eur. Phys. J. D*, 2005, **34**, 19–22.

84 R. Fournier, *J. Chem. Phys.*, 2001, **115**, 2165–2177.

85 S. Yasumura, T. Kato, T. Toyao, Z. Maeno and K.-I. Shimizu, *Phys. Chem. Chem. Phys.*, 2023, **25**, 8524–8531.

86 W. Wang, X. Liu and J. Pérez-Ros, *J. Phys. Chem. A*, 2021, **125**, 5670–5680.

87 M. N. Collacique, V. K. Ocampo-Restrepo and J. L. F. Da Silva, *J. Chem. Phys.*, 2022, **156**, 124106.

88 Y.-X. Yu, *J. Colloid Interface Sci.*, 2025, **695**, 137799.

